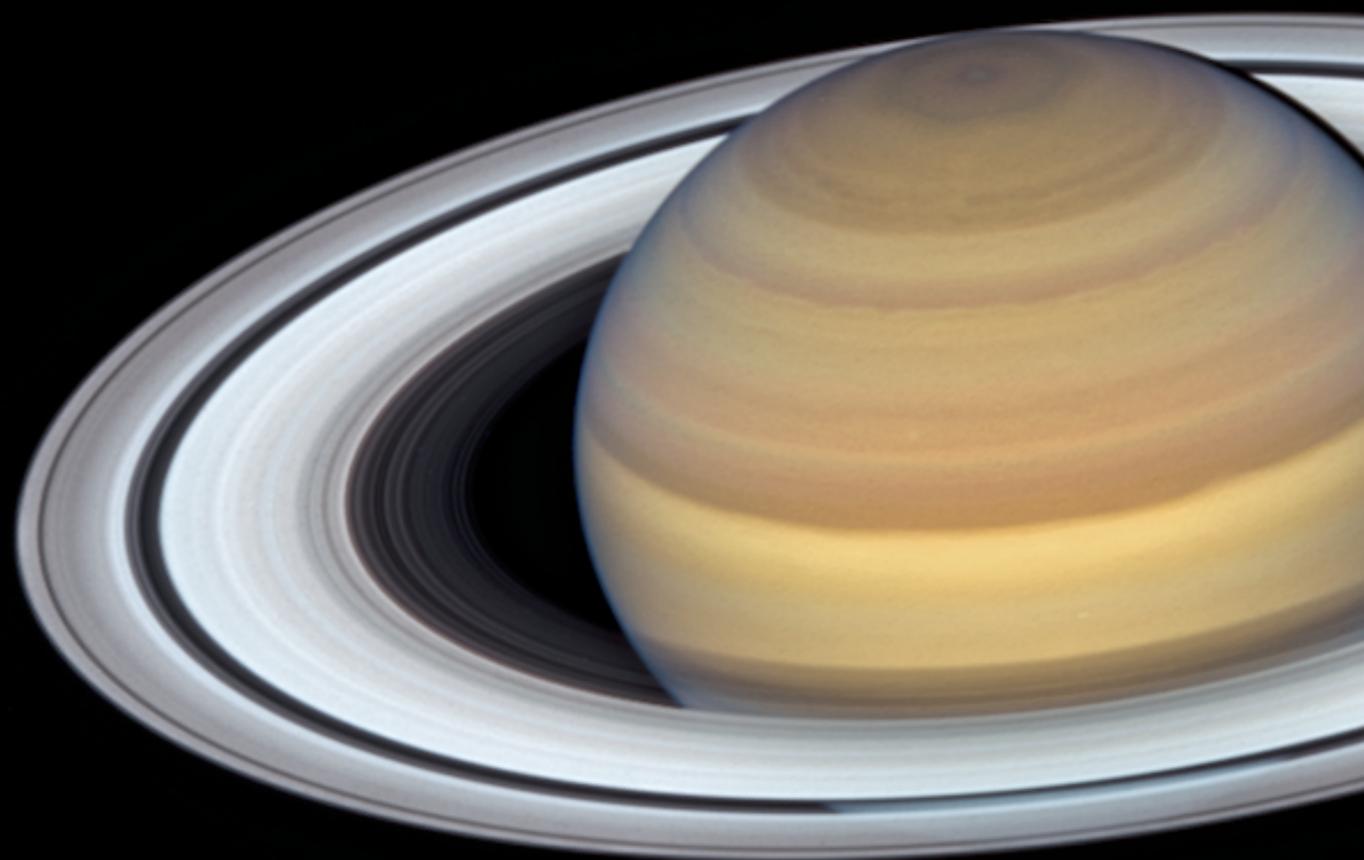
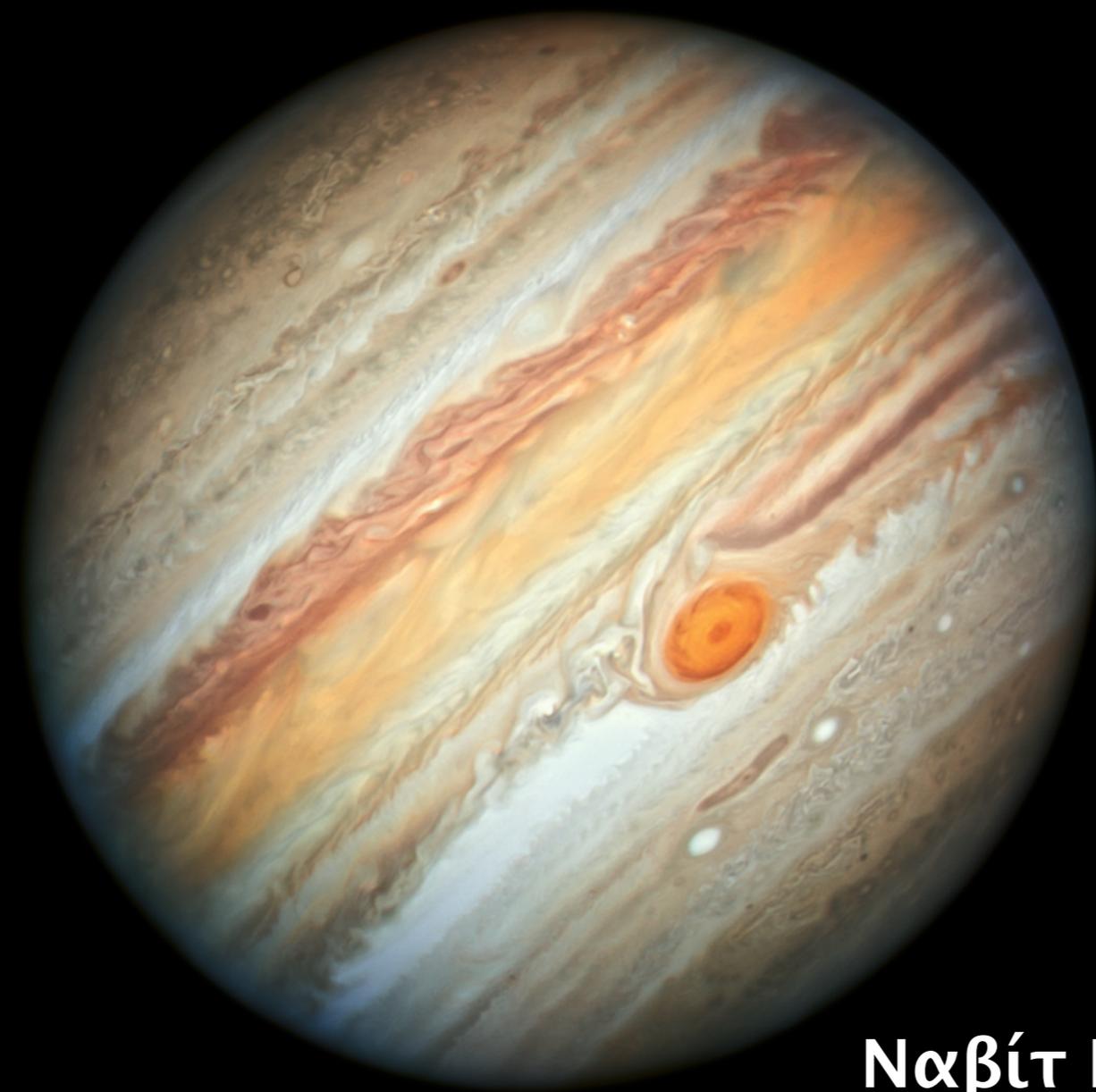


# Τι κρύβεται κάτω από τις ζώνες του Δία και του Κρόνου;



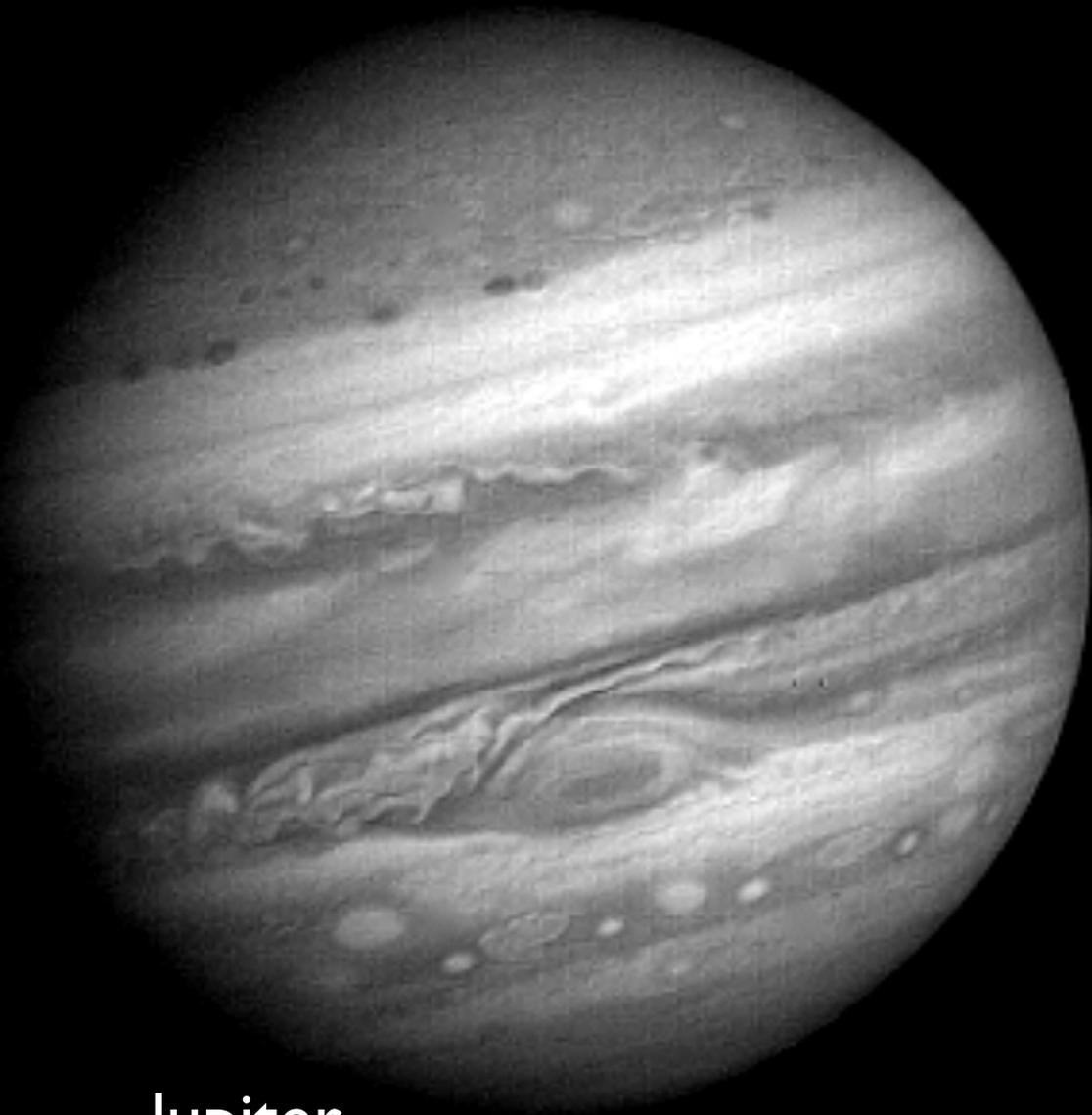
Δίας  
Hubble telescope, NASA  
(Αυγ 2019)

**Ναβίτ Κωνσταντίνου**

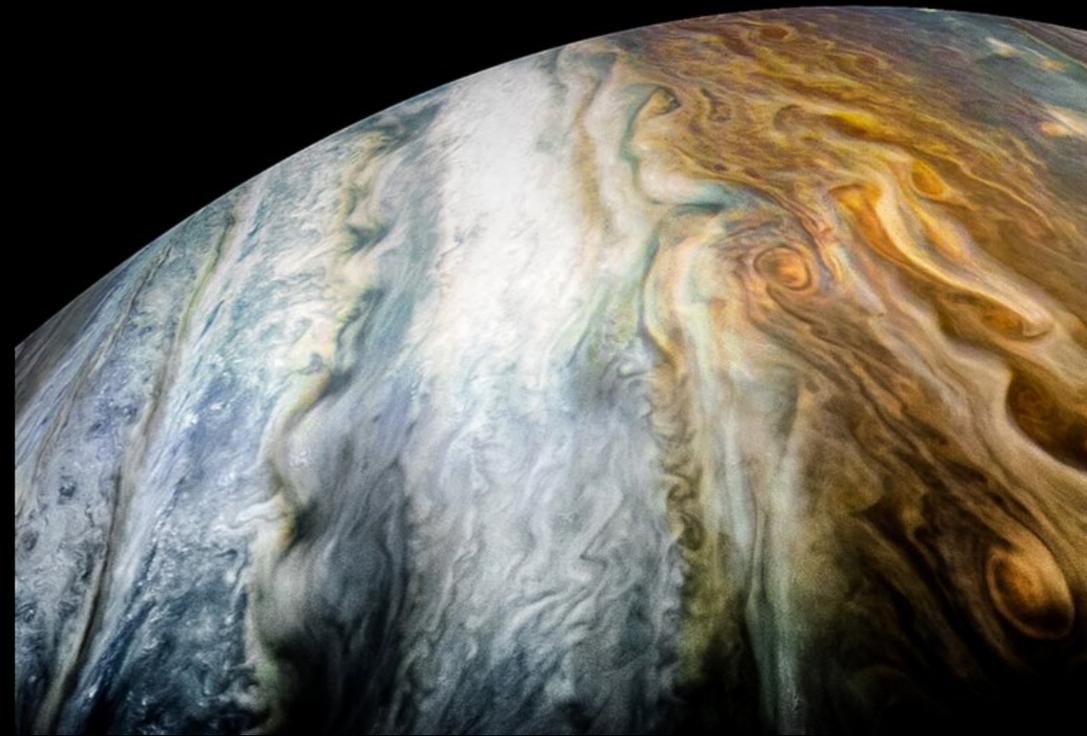
Σεμινάριο Τμήματος Φυσικής  
16 Οκτωβρίου 2019

Κρόνος  
Hubble telescope, NASA  
(Σεπ 2019)

jets coexist with vigorous turbulence



Jupiter  
by *Voyager*  
(1980)



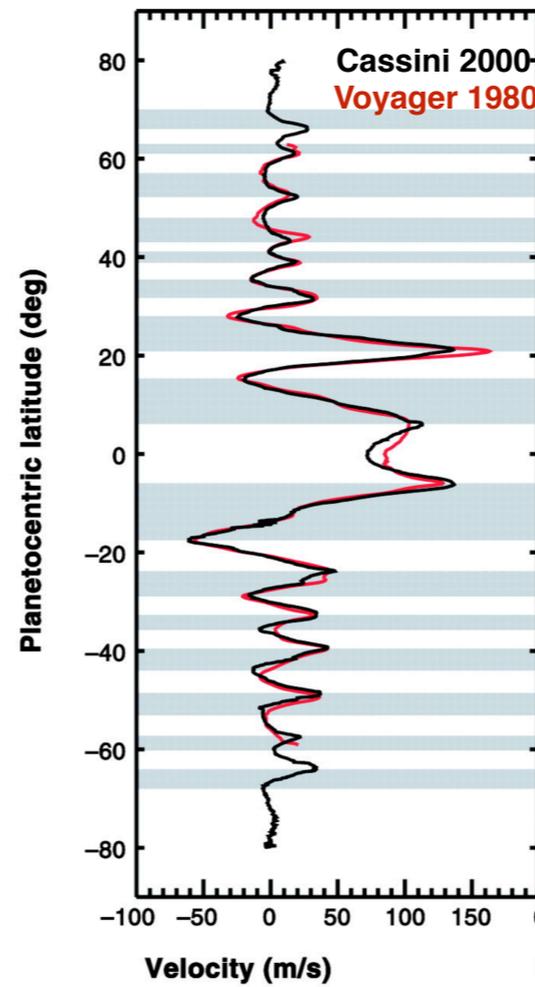
Jupiter  
by *Juno*  
(2015)

jets appear to be "steady"

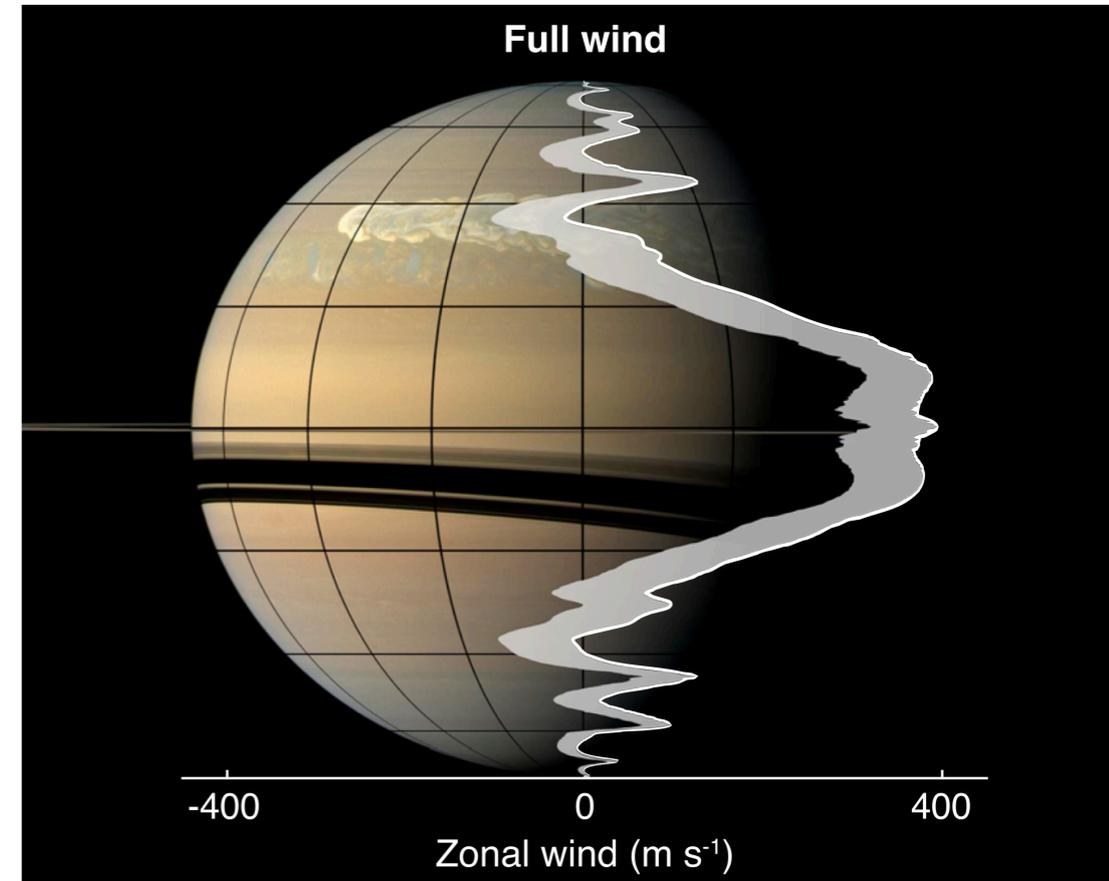
Jupiter



Jovian winds



Saturn



# towards a theory for understanding outer-atmosphere jets

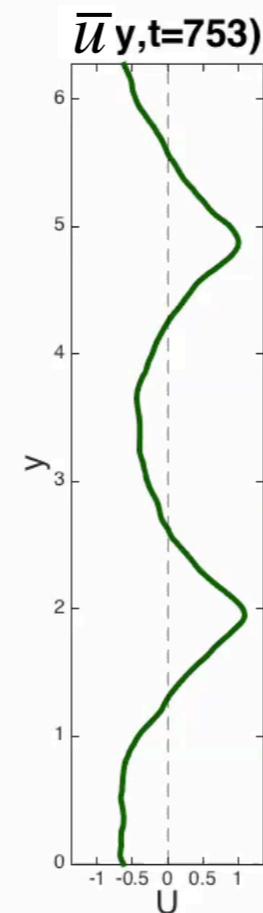


$$\mathbf{u} = (u(x, t), v(x, t))$$

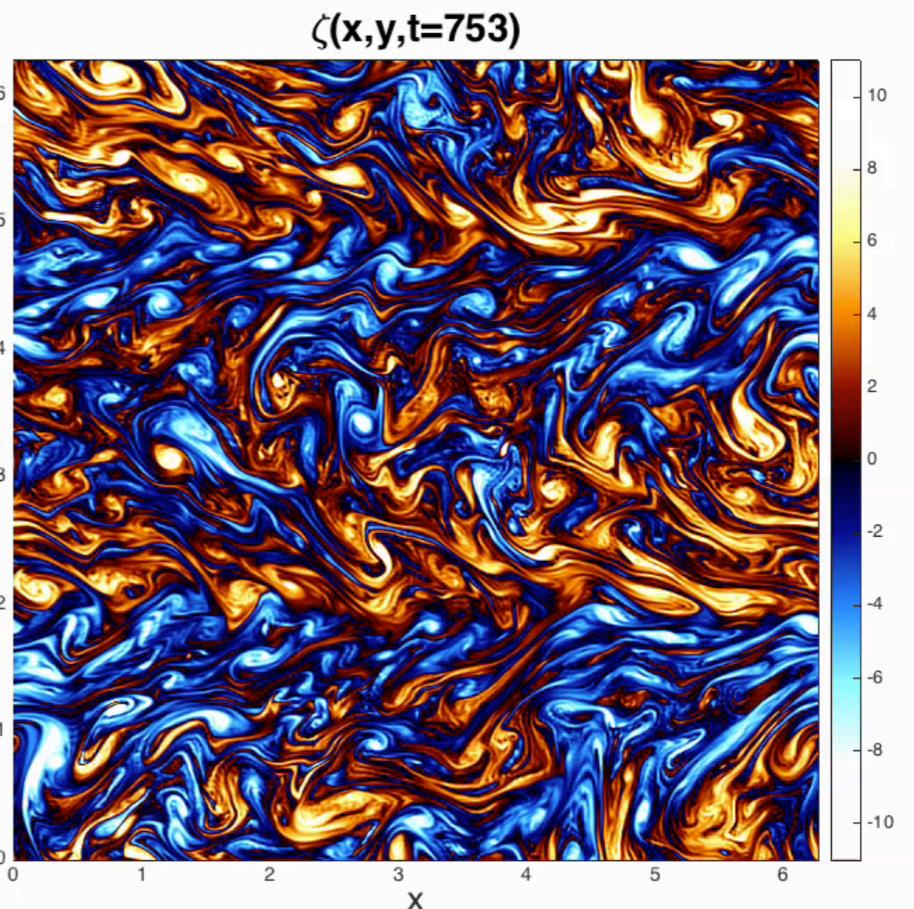
$$\mathbf{u} = \underbrace{\bar{\mathbf{u}}}_{\text{jets}} + \underbrace{\mathbf{u}'}_{\substack{\text{eddies} \\ (=turbulence)}}$$

$$\bar{\mathbf{u}} \equiv \frac{1}{L_x} \int_0^{L_x} \mathbf{u} \, dx$$

zonal mean  $u$



vorticity  $\zeta = \partial_x v - \partial_y u$



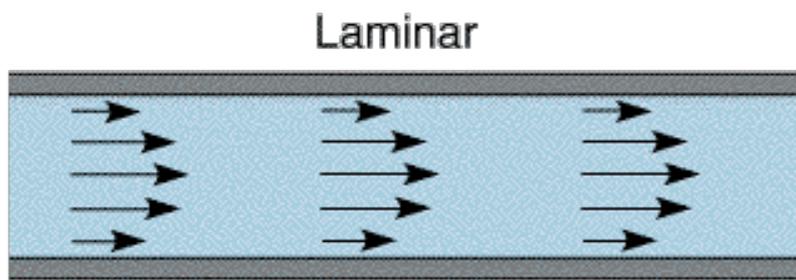
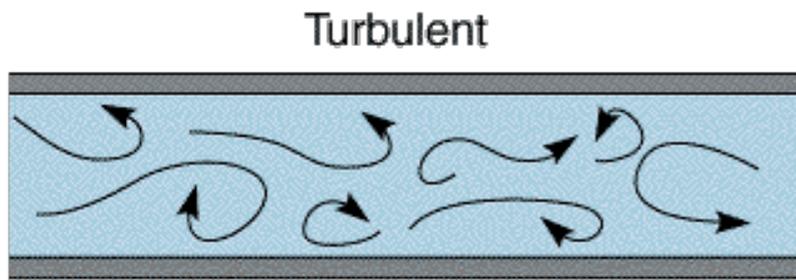
small-scale motions  
self-organise  
to large-scale coherent jets

**How are the zonal jets fueled?**

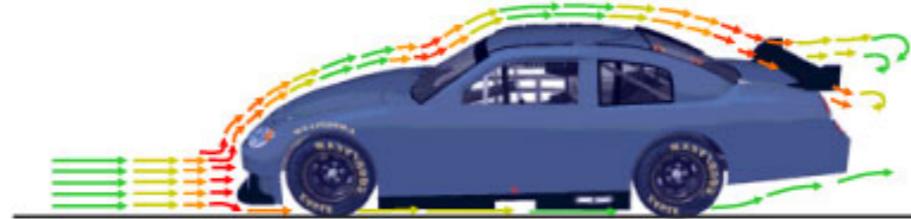
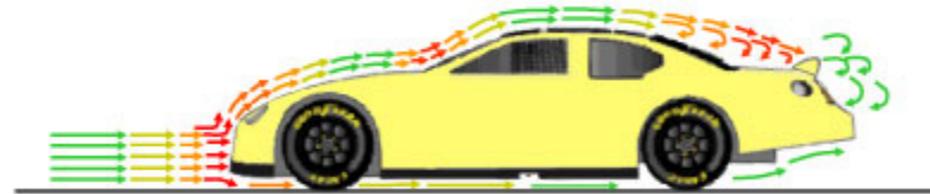
**The eddies (=turbulence) feed  
the jets with momentum!**



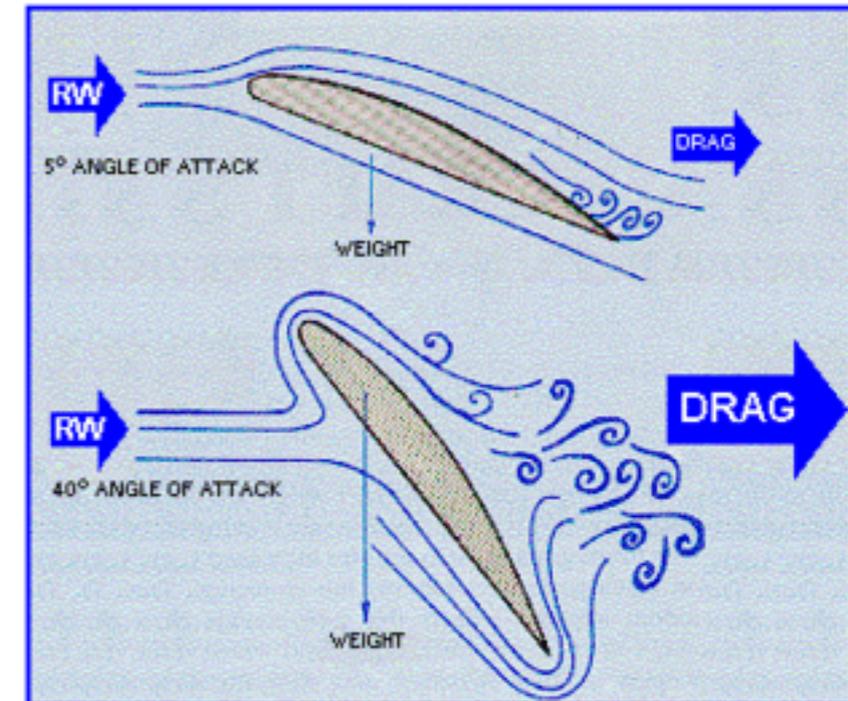
# turbulence usually acts as drag



wall-bounded  
flow



airflow over  
vehicle



airflow over airfoil

Can turbulence act to **reinforce** flows?

# towards a theory for understanding outer-atmosphere jets



Navier-Stokes eq. for incompressible fluid  
(Newton's 2nd law)

$$\rho \left( \frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} \right) = \underbrace{-\nabla \phi}_{\text{reduced pressure gradient}} - \underbrace{2\rho \boldsymbol{\Omega} \times \mathbf{u}}_{\text{Coriolis force}} + \underbrace{\nu \rho \nabla^2 \mathbf{u}}_{\text{viscosity (dissipation)}} + \underbrace{\boldsymbol{\xi}}_{\text{forcing (small-scale noise; } \overline{\boldsymbol{\xi}} = 0)}$$

$\underbrace{\rho \left( \frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} \right)}_{\text{mass} \times \text{acceleration}} = \underbrace{-\nabla \phi - 2\rho \boldsymbol{\Omega} \times \mathbf{u} + \nu \rho \nabla^2 \mathbf{u} + \boldsymbol{\xi}}_{\text{“forces”}}$

$$\mathbf{x} = (x, y)$$

$$\mathbf{u} = (u(x, t), v(x, t))$$

after some fiddling:

$$\frac{\partial \bar{u}}{\partial t} = - \frac{\partial \overline{u'v'}}{\partial y} + \nu \nabla^2 \bar{u}$$

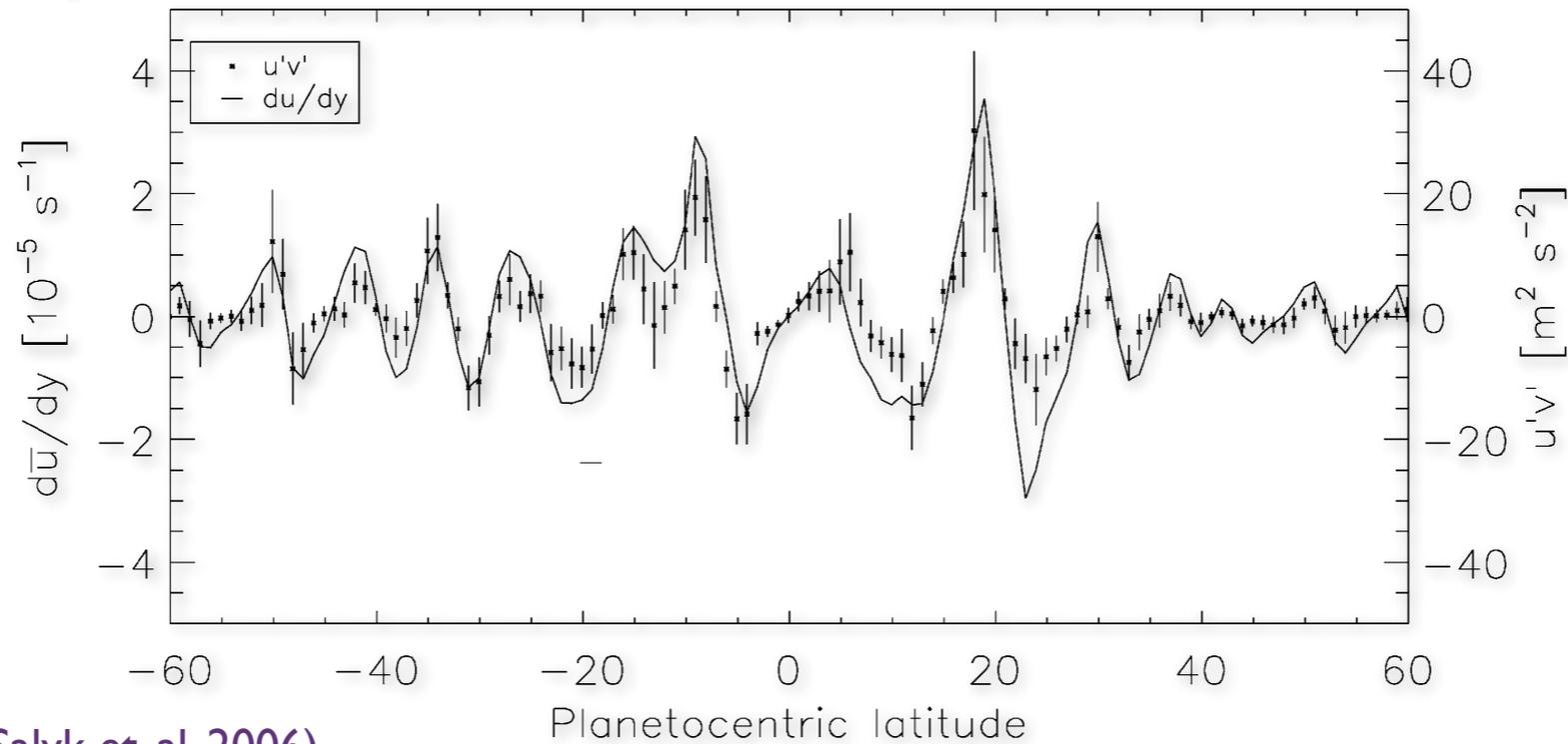
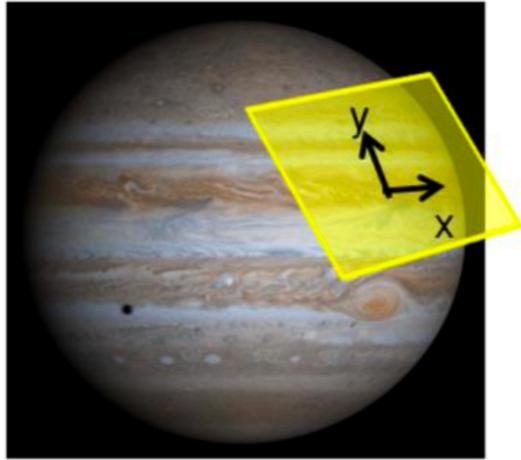
Reynolds stresses
viscosity

(divergence of energy-momentum tensor)

$$\mathbf{u} = \bar{\mathbf{u}} + \mathbf{u}'$$

jets
eddies (=turbulence)

# jets are eddy-driven



(Salyk et. al. 2006)

$$\overline{u'v'} \approx \kappa \frac{\partial \bar{u}}{\partial y}$$

$$\kappa \approx 10^6 \text{ m}^2 \text{ s}^{-1}$$

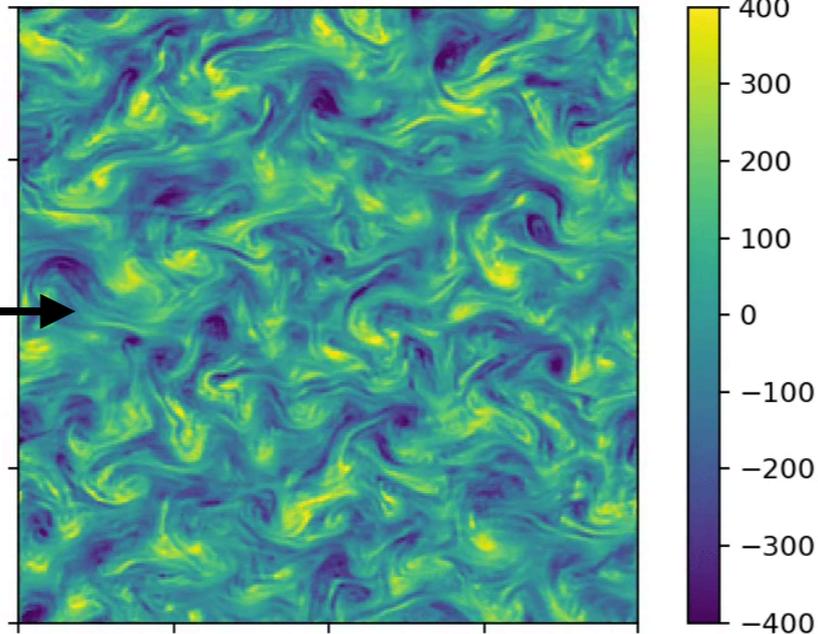
$$\frac{\partial \bar{u}}{\partial t} = - \frac{\partial}{\partial y} \overline{u'v'} = \frac{\partial}{\partial y} \left( - \kappa \frac{\partial \bar{u}}{\partial y} \right) \text{ anti-diffusion (or negative viscosity)}$$

# how can we perform stability of turbulent flows?

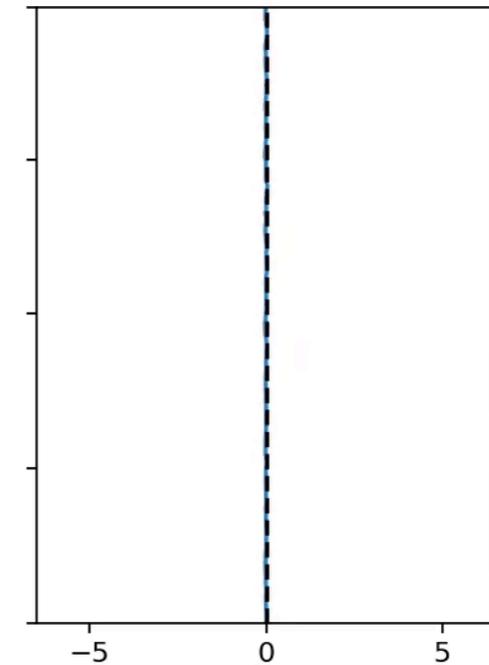
how do we show that a flow like this ...

[simulation in which at each time step we "kill" the zonal-mean component]

vorticity  $(\partial_x v - \partial_y u)/\mu$  at  $\mu t = 5.00$

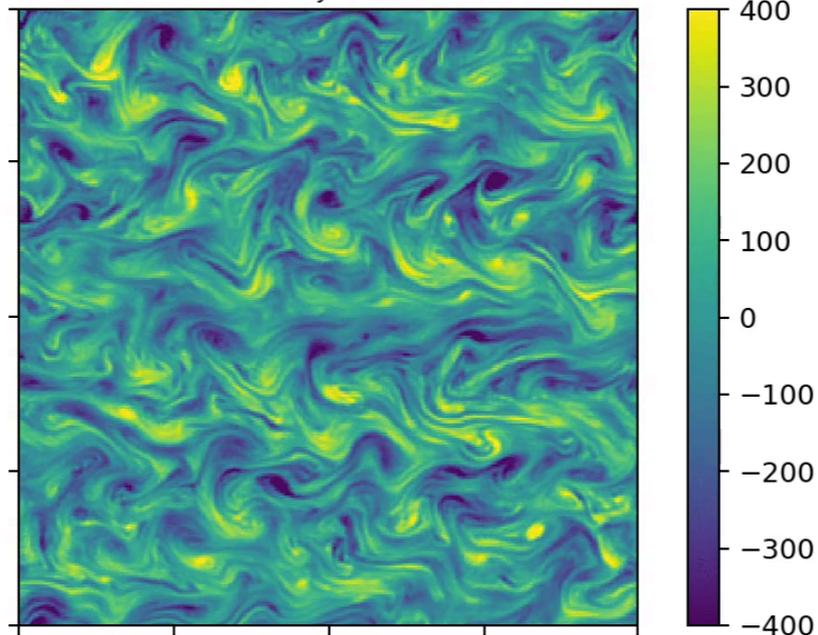


zonal mean  $\bar{u}/(\beta k_f^{-2})$  at  $\mu t = 5.00$

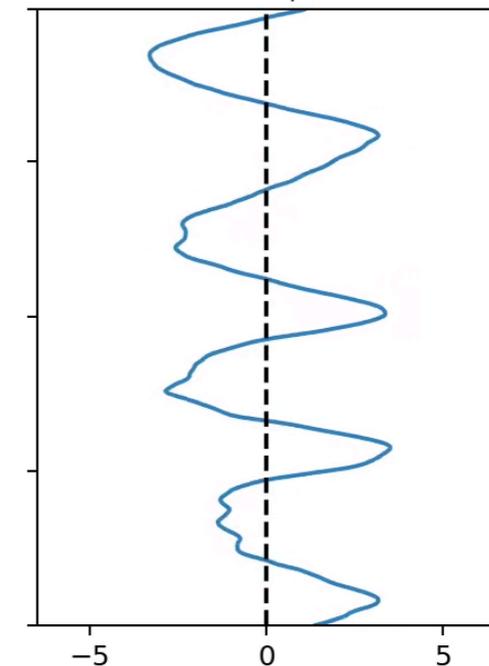


... is **unstable** leading to forming four jets?

vorticity  $(\partial_x v - \partial_y u)/\mu$  at  $\mu t = 5.00$



zonal mean  $\bar{u}/(\beta k_f^{-2})$  at  $\mu t = 5.00$



# the need for a new framework

To understand the underlying dynamics of jet formation  
we need to change framework...

dynamics of flow  
realizations  
(e.g. Navier-Stokes, ...)

$$u(x, t), \dots$$



**dynamics** that govern  
the same-time statistics  
of the flow fields

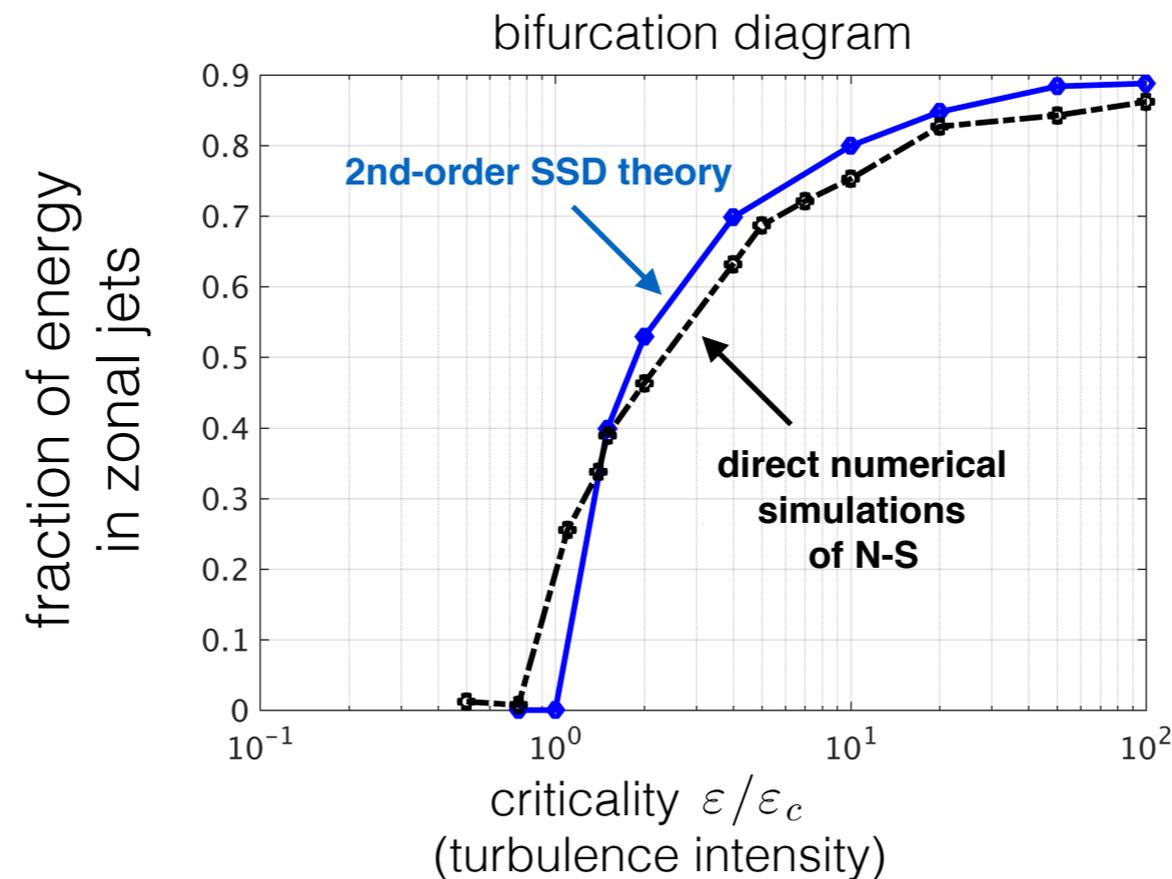
$$\overline{u(x, t)}, \overline{u'(x_1, t)u'(x_2, t)}, \dots$$

**Statistical State Dynamics**

Farrell & Ioannou (2003) *JAS*

Statistical State Dynamics allows us linearize about a turbulent flow!

# outer-atmosphere jets [a theory for their formation]



jets emerge  
through a "phase change"  
that occurs as  
turbulence intensity increases

Flow realizations (dns) exhibit jet formation,  
**but** its analytic expression appears only the SSD.

Predicting  $\varepsilon_c$  or the structure of the emergent jet is  
**not** possible through N-S dynamics.

**We understand how outer-atmosphere  
jet form and maintain.**

**But what's happening below the clouds?**

**For example: how deep these jets  
continue below the clouds?**

# how deep the jets go below the clouds?

outstanding question

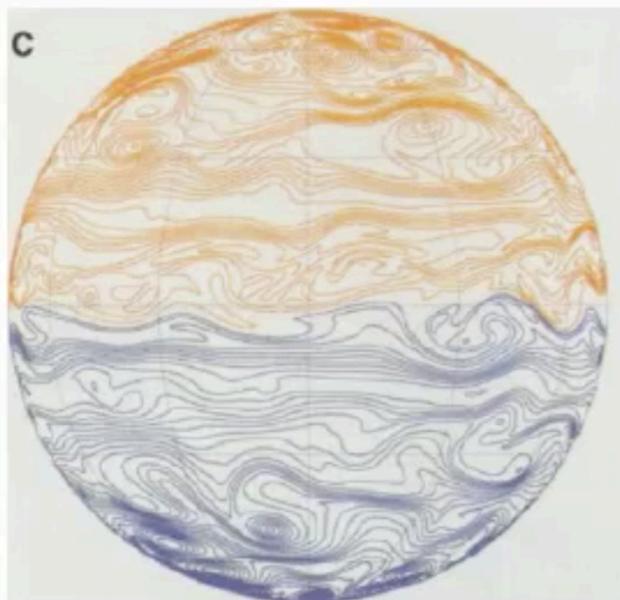
rooted deep in debate among various theories

*shallow-jet theories*

jets exist only within  
the top-atmospheric layer ~100km

*deep-jet theories*

jets reach the centre of the planet  
"Taylor columns"



Shallow geostrophic turbulence  
(Rhines, 1975, Cho & Polvani 1996)

**Shallow or deep?**



Deep internal convection  
(Busse, 1976, Heimpel et al, 2005  
Fig. from Ingersoll, 1990)

**spacecraft *Juno*  
was launched in 2011  
and entered orbit  
around Jupiter in 2015**

**JUNO**



# *Juno's mission*

2016-07-01 00:00

Juno

make detailed measurements of  
Jupiter's **gravitational** and  
**magnetic** fields

Jupiter



Jupiter's background radiation is ***EXTREME!***  
(around  $5 \times 10^7$  times stronger of that here on Earth)

Strategy: Go in close; get the data; get out quick!

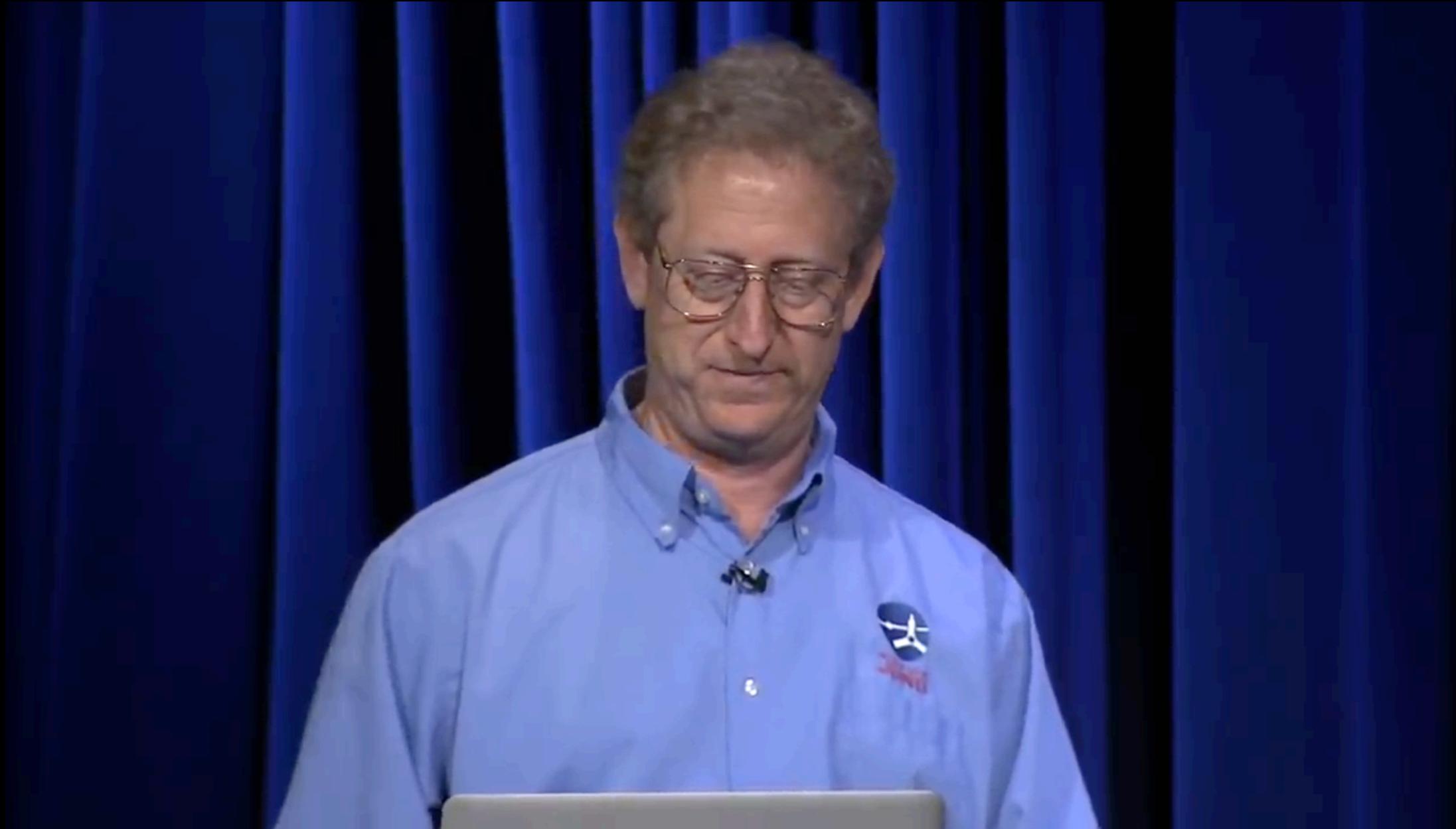
0.00km/s

4,469,608km

At its closest point it reaches  
only ~4500km over the cloud tops  
(that's about the distance from Athens to Iceland)

# What did *Juno* discover?

[Excerpt from NASA Jet Propulsion Laboratory public announcement, May 2018]



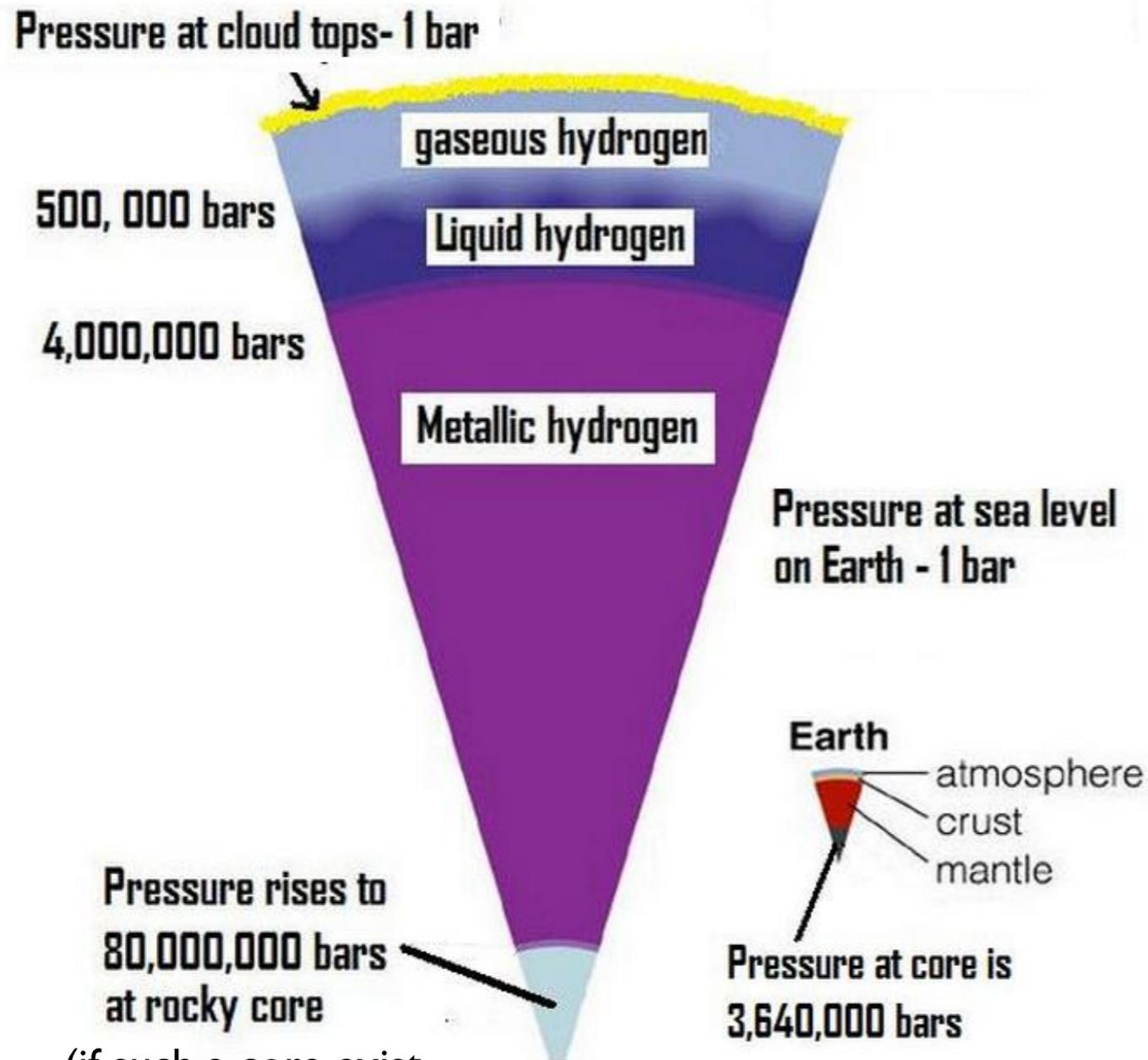
Dr. Steve Levin

*Juno* Project Scientist  
NASA JPL

*"...magnetic field has something to do with why the belts and zones only go that deep (...)  
But we don't know this yet; **it's speculation.**"*

# deep inside the gas giants fluid becomes conducting

CROSS SECTION OF JUPITER



(if such a core exist  
*Juno's* findings suggest  
there is no rocky core)

as we go deeper inside Jupiter  
pressure rises **dramatically**

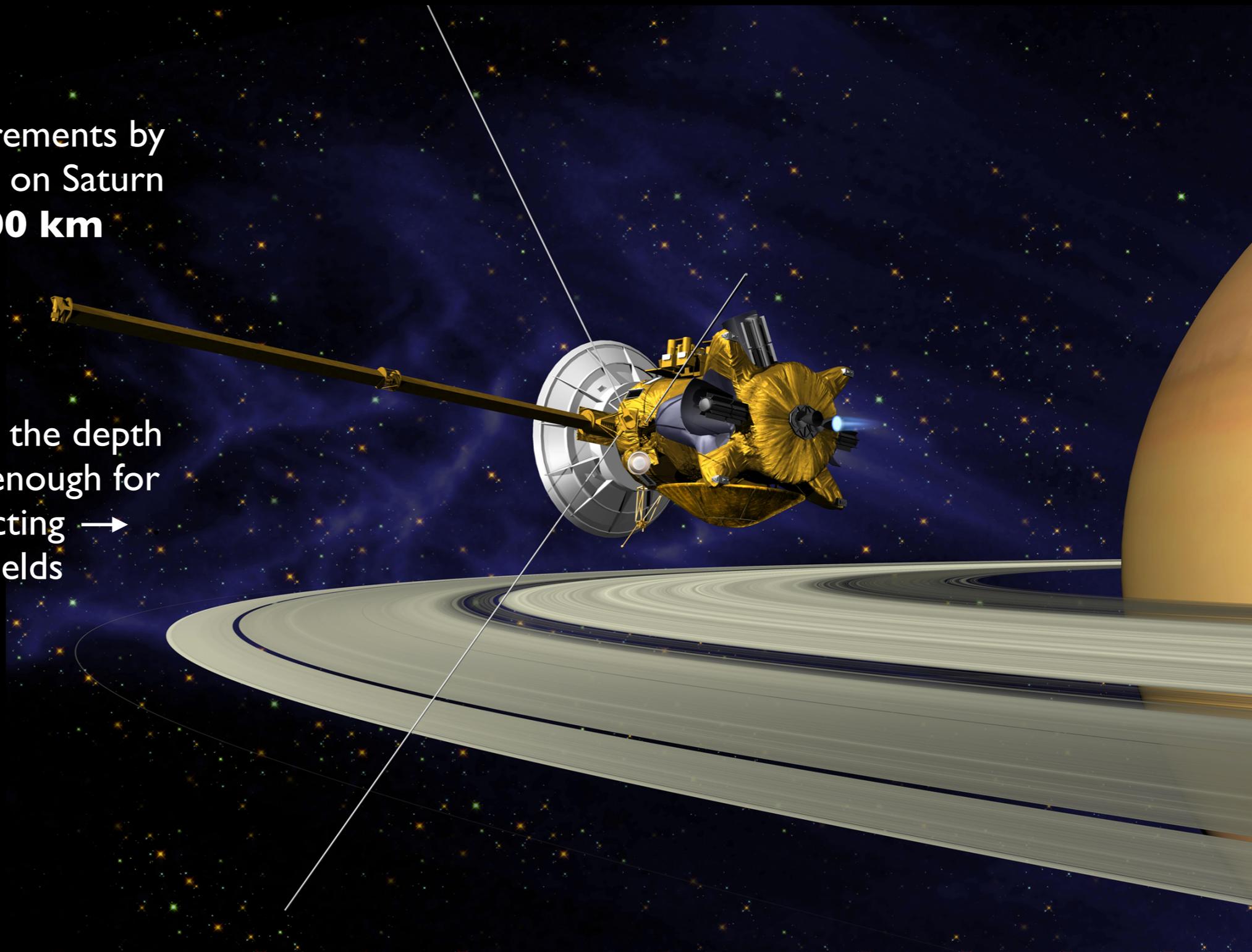
electrons escape the molecules  
and the fluid **becomes conducting**

conducting moving fluid →  
→ currents → magnetic fields

# Btw, same story in Saturn...

Gravitometric measurements by *Cassini* reveal that jets on Saturn go as deep as **8500 km**

and again that's about the depth that pressure is high enough for the fluid to be conducting →  
→ magnetic fields



here's where me and Jeff Parker come into the story..



Jeffrey Parker  
Lawrence Livermore  
National Laboratory  
CA, USA

# Magnetic fields bring about new terms in equations of motion

**N-S → MHD**

$$\rho \frac{\partial u}{\partial t} + \dots = \underbrace{J \times B}_{\text{Lorentz force}} + \dots$$

$$\frac{\partial B}{\partial t} = \dots \quad B = (B_x, B_y)$$

induction equation  
Faraday's law

$$\mu_0 \mathbf{J} = \nabla \times \mathbf{B} \quad \text{Ampère's law (ignoring displacement current)}$$

[... some fiddling]  
now zonal flow obeys:

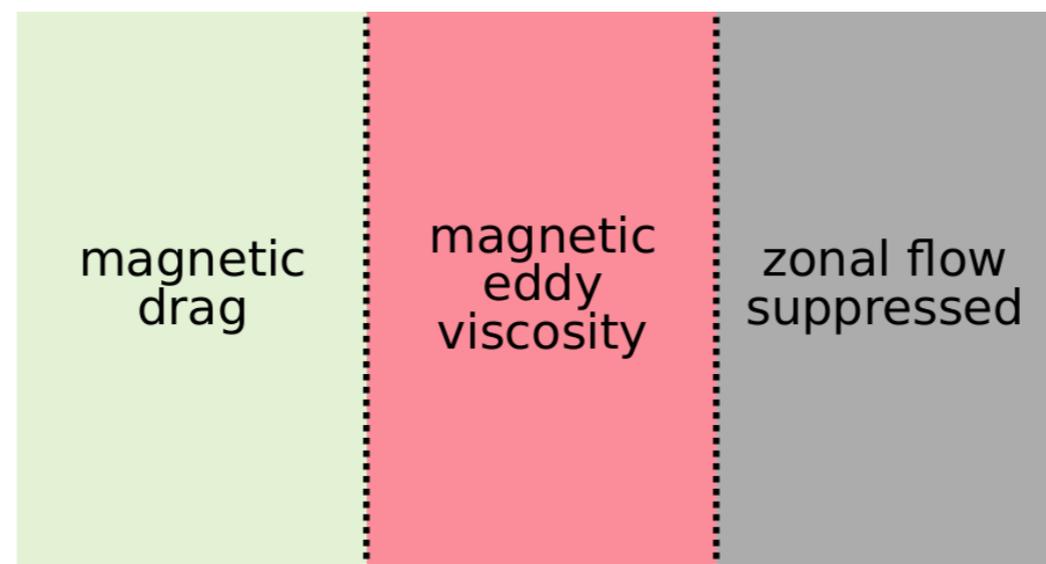
$$\frac{\partial \overline{\rho u}}{\partial t} = \underbrace{\frac{1}{\mu_0} \frac{\partial \overline{B'_x B'_y}}{\partial y}}_{\text{Maxwell stresses}} - \underbrace{\frac{\partial \overline{\rho u' v'}}{\partial y}}_{\text{Reynolds stresses}} + \text{dissipation}$$

# We point out a new regime of *magnetic eddy viscosity*

Collective effect of a mean shear flow to the magnetic fluctuations acts effectively to increase the fluid's viscosity

$$\mathcal{A} = \frac{|\mathbf{J} \times \mathbf{B}|}{|\rho \mathbf{u} \cdot \nabla \mathbf{u}|}$$

$$= \frac{\text{Lorentz force}}{\text{inertial force}}$$



$$\text{Rm} = \frac{LV}{\eta} \rightarrow \text{magnetic diffusivity}$$

$$= \frac{\text{inertial force}}{\text{viscous force}}$$

$\text{Rm} = 1,$   
 $\mathcal{A} \ll 1$

$\mathcal{A} = 1$

this is exactly the regime where zonal jets start being suppressed

# We point out a new regime of *magnetic eddy viscosity*

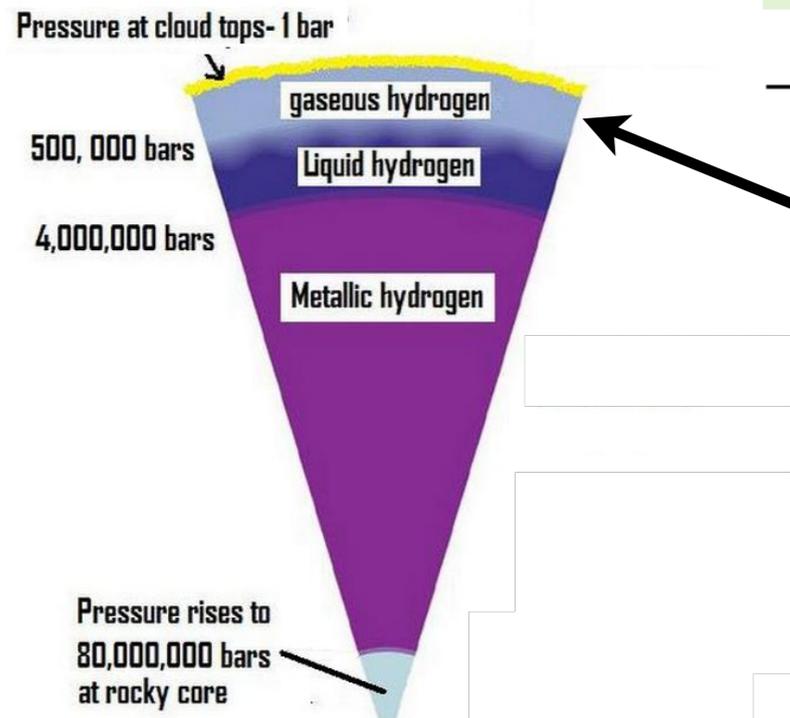
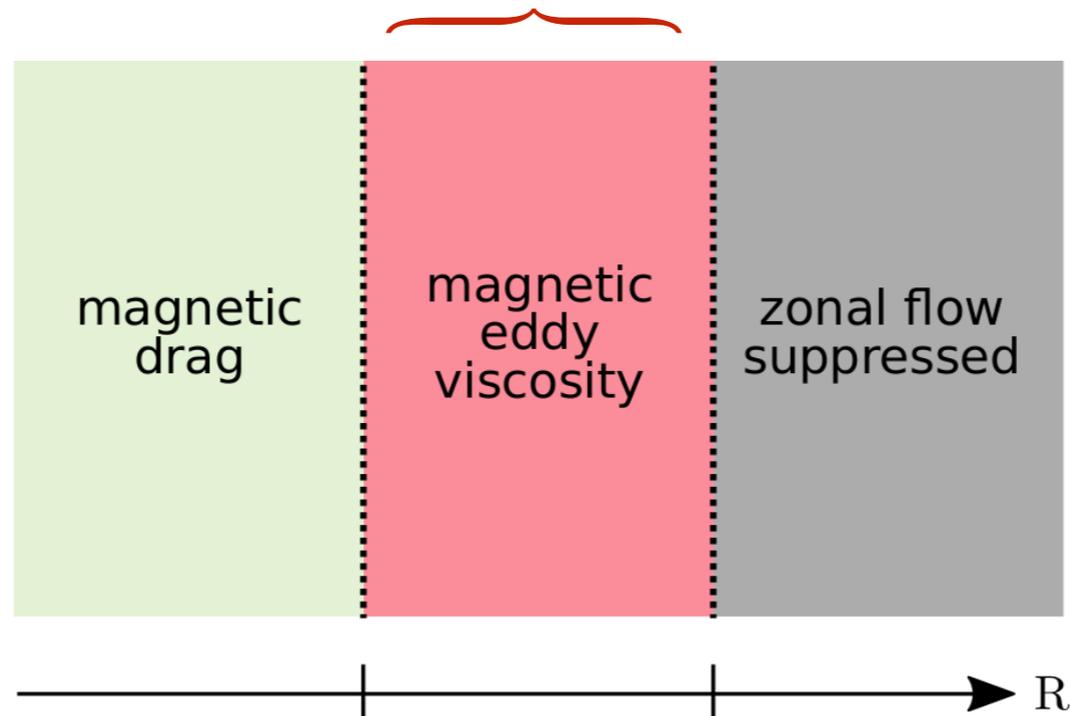
Collective effect of a mean shear flow to the magnetic fluctuations acts effectively to increase the fluid's viscosity

$$\mathcal{A} = \frac{|J \times B|}{|\rho u \cdot \nabla u|}$$

$$= \frac{\text{Lorentz force}}{\text{inertial force}}$$

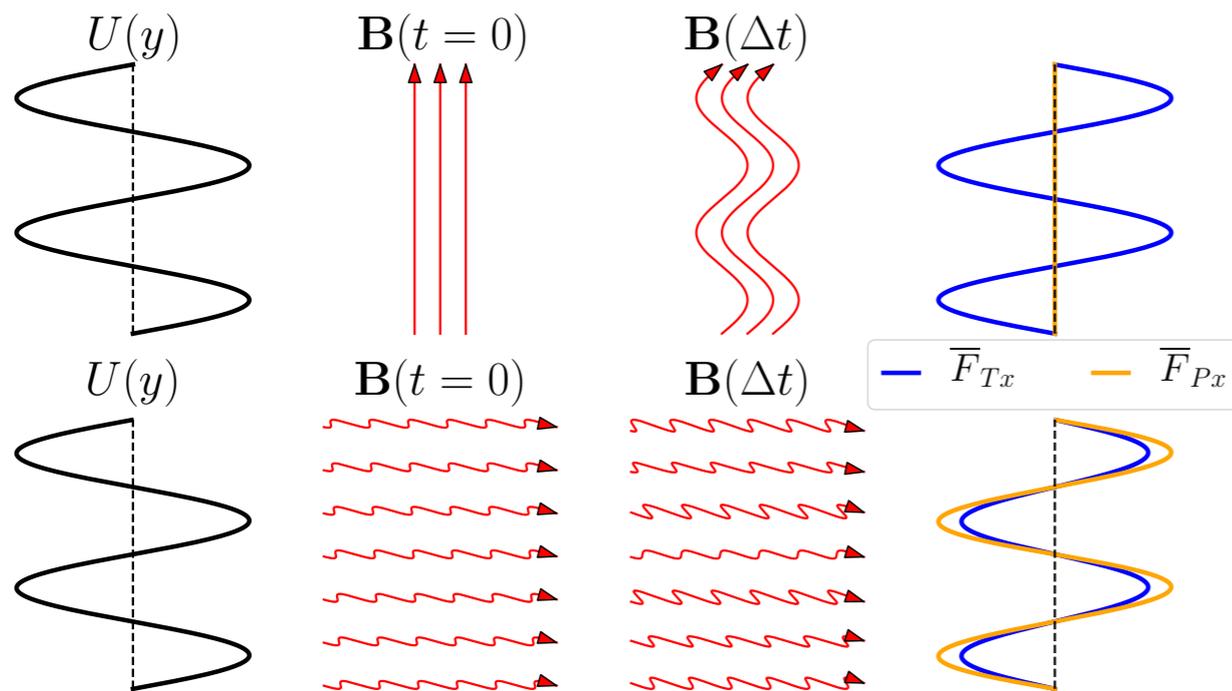
$$Rm = \frac{LV}{\eta} \rightarrow \text{magnetic diffusivity}$$

$$= \frac{\text{inertial force}}{\text{viscous force}}$$



this is exactly the regime where zonal jets start being suppressed

# We derive magnetic viscosity from simple physical arguments



$$u(t = 0) \text{ \& } U(y) \longrightarrow \Delta \overline{uv} \propto \Delta t \overline{v^2} \partial_y U$$

$$\implies -\partial_y \overline{uv} = \underbrace{\partial_y [-\gamma \Delta t \overline{v^2} \partial_y U]}$$

**negative turbulent viscosity**

$$B(t = 0) \text{ \& } U(y) \longrightarrow \Delta \overline{B_x B_y} \propto \overline{B_y^2} \partial_y U$$

$$\implies \frac{1}{\mu_0} \partial_y \overline{B_x B_y} = \partial_y \left[ \underbrace{\alpha \frac{1}{\mu_0} \Delta t \overline{B_y^2} \partial_y U} \right]$$

**magnetic viscosity**

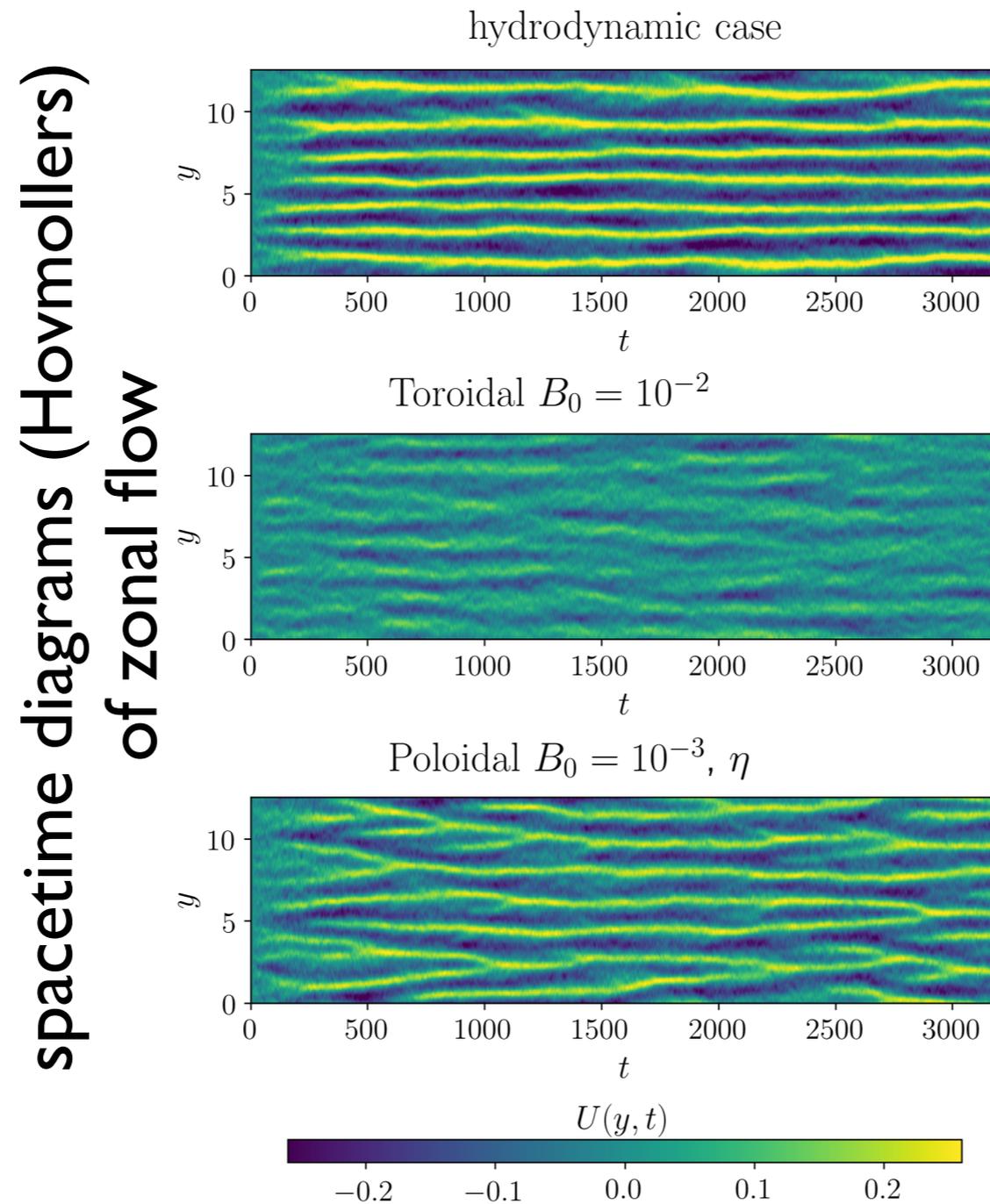
$\alpha, \gamma = \text{nondim constants of } O(1)$

# Putting it all together

zonal flow  
equation:

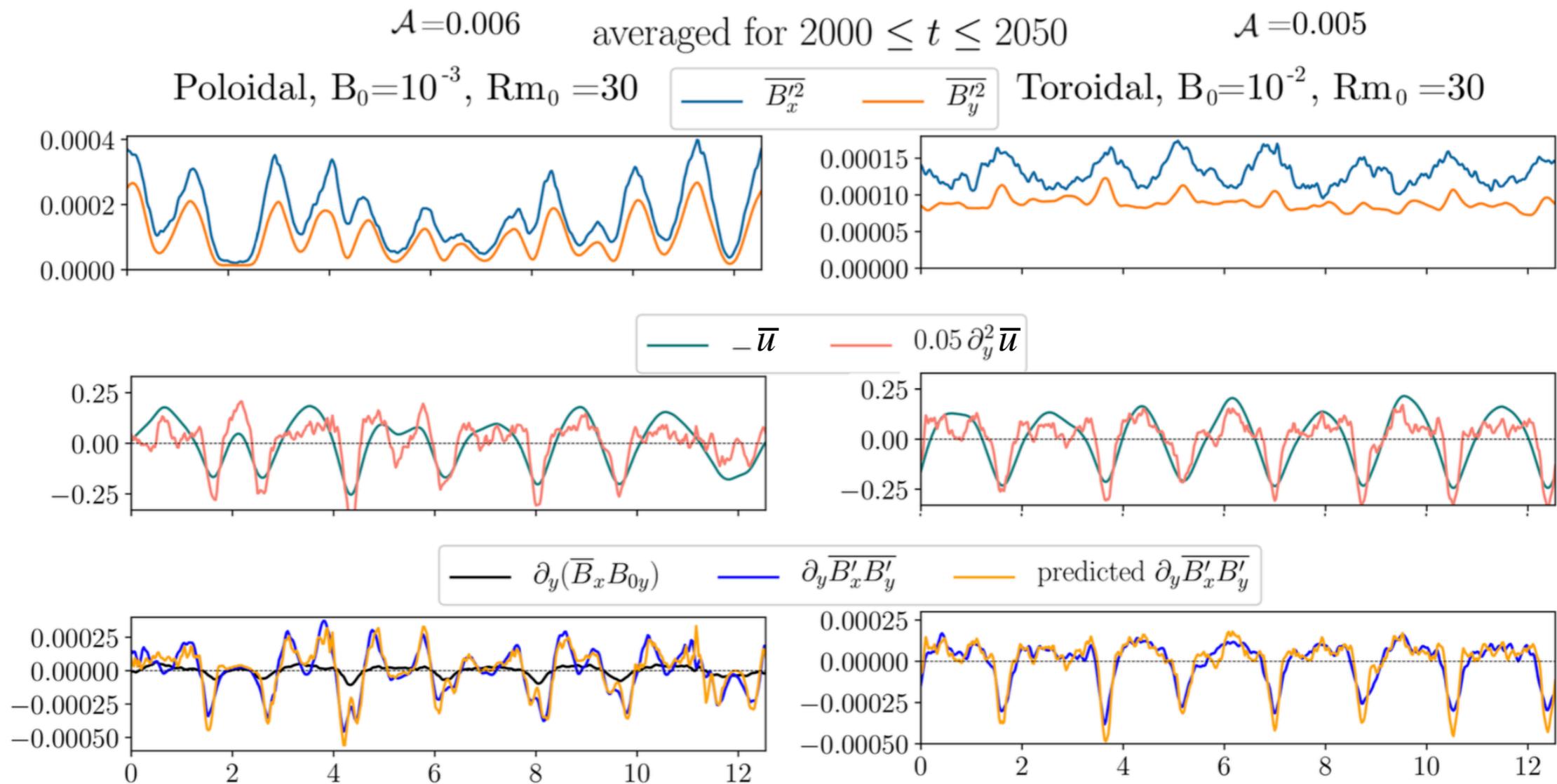
$$\begin{aligned}\frac{\partial \bar{\rho} \bar{u}}{\partial t} &= \frac{1}{\mu_0} \frac{\partial \overline{B'_x B'_y}}{\partial y} - \frac{\partial \overline{\rho u' v'}}{\partial y} + \dots \\ &= \frac{\partial}{\partial y} \left[ \underbrace{\left( \alpha \frac{\overline{B_y^2}}{\mu_0} - \gamma \rho \overline{v'^2} \right) \tau_{\text{corr}}}_{\text{total turbulent viscosity}} \frac{\partial \bar{u}}{\partial y} \right] + \dots\end{aligned}$$

# We verify magnetic viscosity in 2D magnetohydrodynamic simulations



# We verify magnetic viscosity in 2D magnetohydrodynamic simulations

our prediction 
$$\frac{\partial \overline{B'_x B'_y}}{\partial y} = \frac{\partial}{\partial y} \left( \alpha \overline{B_y^2} \tau_{\text{corr}} \frac{\partial \bar{u}}{\partial y} \right)$$



# Ready for a leap of faith?

Use 
$$\frac{\partial \overline{\rho u}}{\partial t} = \frac{\partial}{\partial y} \left[ \left( \alpha \frac{\overline{B_y^2}}{\mu_0} - \gamma \rho \overline{v^2} \right) \tau_{\text{corr}} \frac{\partial \overline{u}}{\partial y} \right] + \dots$$

to predict how deep the jets in Jupiter & Saturn should go.

- ➔ Use typical flow values from cloud tops
- ➔ Use  $B^2 = \text{Rm} B_0^2$  (empirical relation) to get a critical Rm → critical  $\eta$
- ➔ Use current internal structure models for each gas giant to compute the depth that corresponds to the  $\eta_{\text{crit}}$  value

We get: Jupiter 3500 km

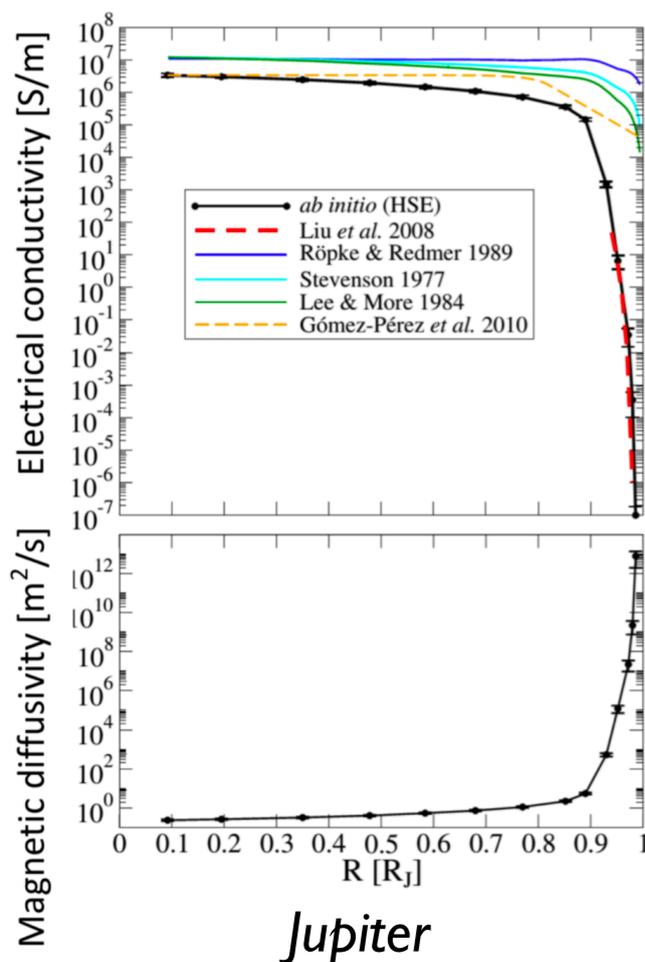
Saturn 8000 km

[*Juno* → Jupiter 3000 km

*Cassini* → Saturn 8500 km]



σύμπτωση;



[French et al., *ApJ Supp. S.* (2012)]

# take home messages

Identified an MHD regime ( $R_m \gg 1$  &  $\mathcal{A} \ll 1$ ) in which there is *magnetic eddy viscosity* of mean shear flow

Simple derivation with clear physical picture:

Shear flow + MHD frozen-in law + “short” decorrelation due to turbulence

Confirmed in 2D incompressible MHD simulations

Magnetic eddy viscosity provides a plausible explanation for the depth-extent of the zonal jets in Jupiter and Saturn

*ευχαριστώ*

Constantinou and Parker (2018). Magnetic suppression of zonal flows on a beta plane. *Astrophysical Journal*, **863**, 46.

Parker and Constantinou (2019). Magnetic eddy viscosity of mean shear flows in two-dimensional magnetohydrodynamics. *Physical Review Fluids*, **4**, 083701

Constantinou (2018). Jupiter’s magnetic fields may stop its wind bands from going deep into the gas giant, *The Conversation*, August 10th , 2018