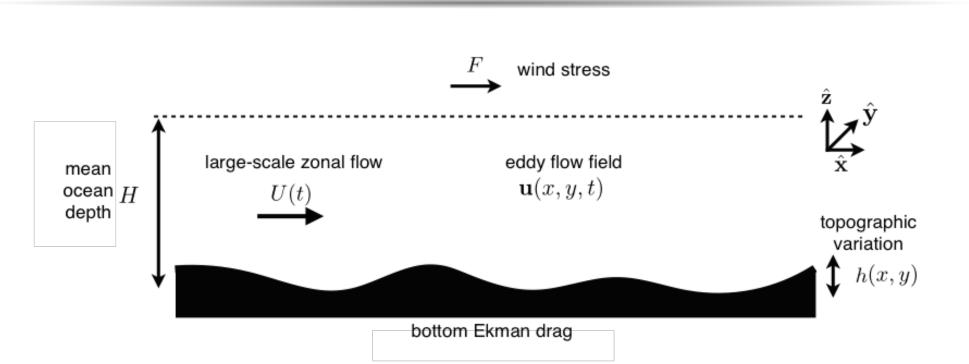


Objectives

Study the regimes of geostrophic turbulence above topography when forced by steady wind stress.

- How much momentum input by the wind stress is balanced by bottom drag, and how much by topographic form stress?
- What topographic features affect the large-scale flow?
- How does the mass transport depend on wind stress?

Model



The simplest model of topographic form stress:

Single-layer quasi-geostrophic setting, forced by a steady zonal mean wind stress in a doubly periodic domain of size $2\pi L \times 2\pi L$. Flow consists of:

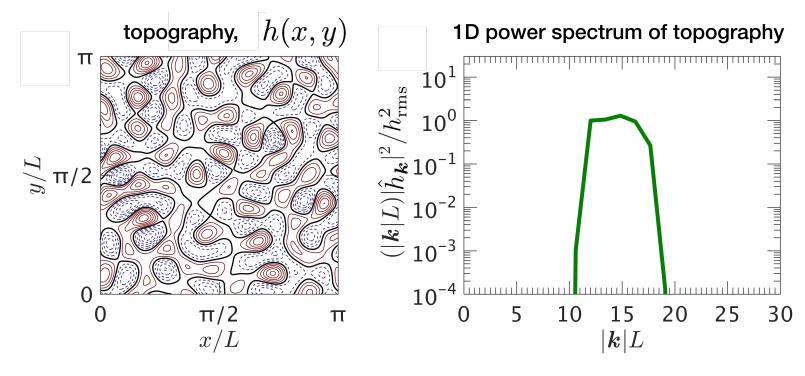
- a large-scale zonal mean flow: U(t),
- an eddy flow field: $\psi(x, y, t)$ $(u = -\psi_y, v = \psi_x)$.

Evolution:

$$\nabla^2 \psi_t + \mathsf{J}(\psi - Uy, \nabla^2 \psi + \beta y + \eta) = -\mu \nabla^2 \psi, \qquad (1)$$
$$U_t = F - \mu U - \langle \psi \eta_x \rangle. \qquad (2)$$

- $J(a,b) \stackrel{\text{def}}{=} a_x b_y a_y b_x$: Jacobian,
- μ : Ekman drag coefficient,
- β : planetary vorticity gradient,
- $\langle \psi \eta_x \rangle$: topographic form stress ($\langle \cdot \rangle$ is domain average),
- $F = \tau/(\rho_0 H)$: zonal mean wind stress forcing,
- $\nabla^2 \psi + \beta y + \eta$: quasigeostrophic PV,
- $\eta(x,y) = f_0 h(x,y)/H$: topographic PV,

Flow field can be decomposed into standing (time-mean) and tran*sients*, e.g. $\psi(x, y, t) = \psi(x, y) + \psi'(x, y, t)$.



Properties of topography: homogeneous, isotropic, monoscale,

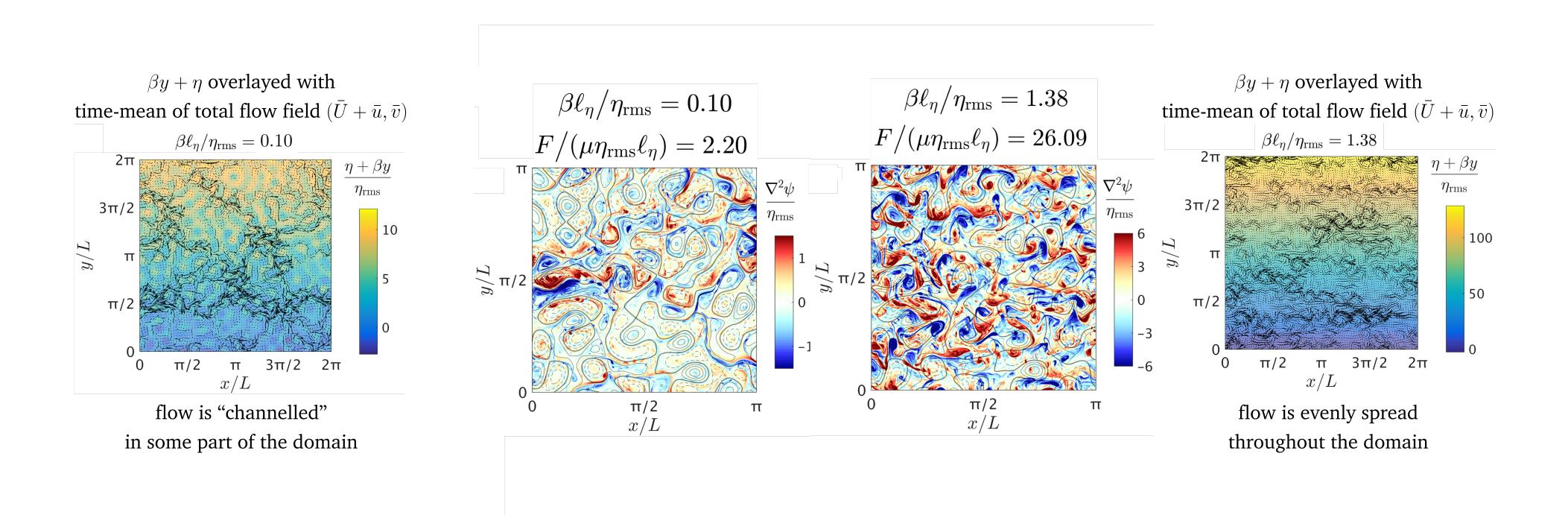
$$\eta_{\rm rms} = \sqrt{\langle \eta^2 \rangle} \ , \ \ell_{\eta} = \sqrt{\frac{\langle \eta^2 \rangle}{\langle |\boldsymbol{\nabla}\eta|^2 \rangle}} \ , \ \frac{L}{\ell_{\eta}} \approx 14.5$$

Three main non-dimensional parameters: $\mu/\eta_{
m rms} = 10^{-2}$ $F/(\mu\eta_{
m rms}\ell_\eta)$ $eta \ell_\eta/\eta_{
m rms}$ dissipation planetary vorticity gradient wind stress forcing

Topographic beta-plane turbulence and form stress

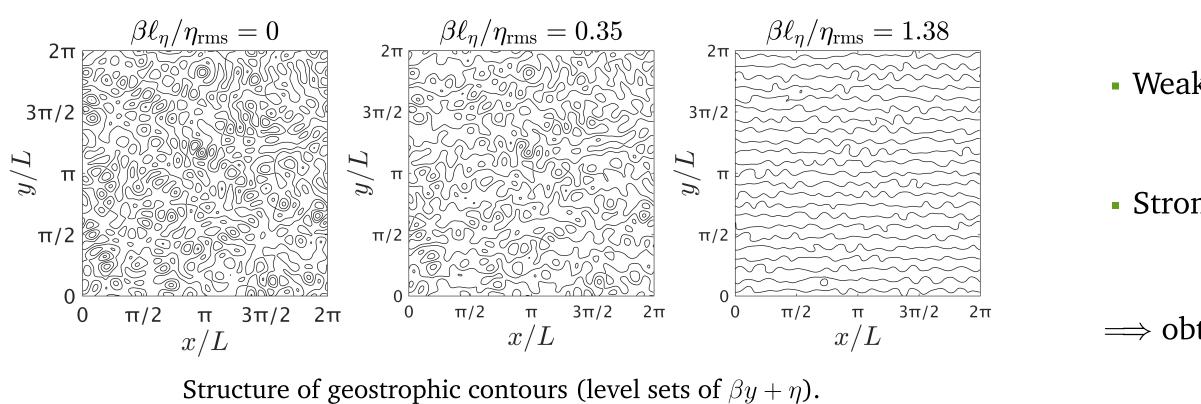
Navid C. Constantinou & William R. Young Scripps Institution of Oceanography, University of California San Diego

Two Flow Examples



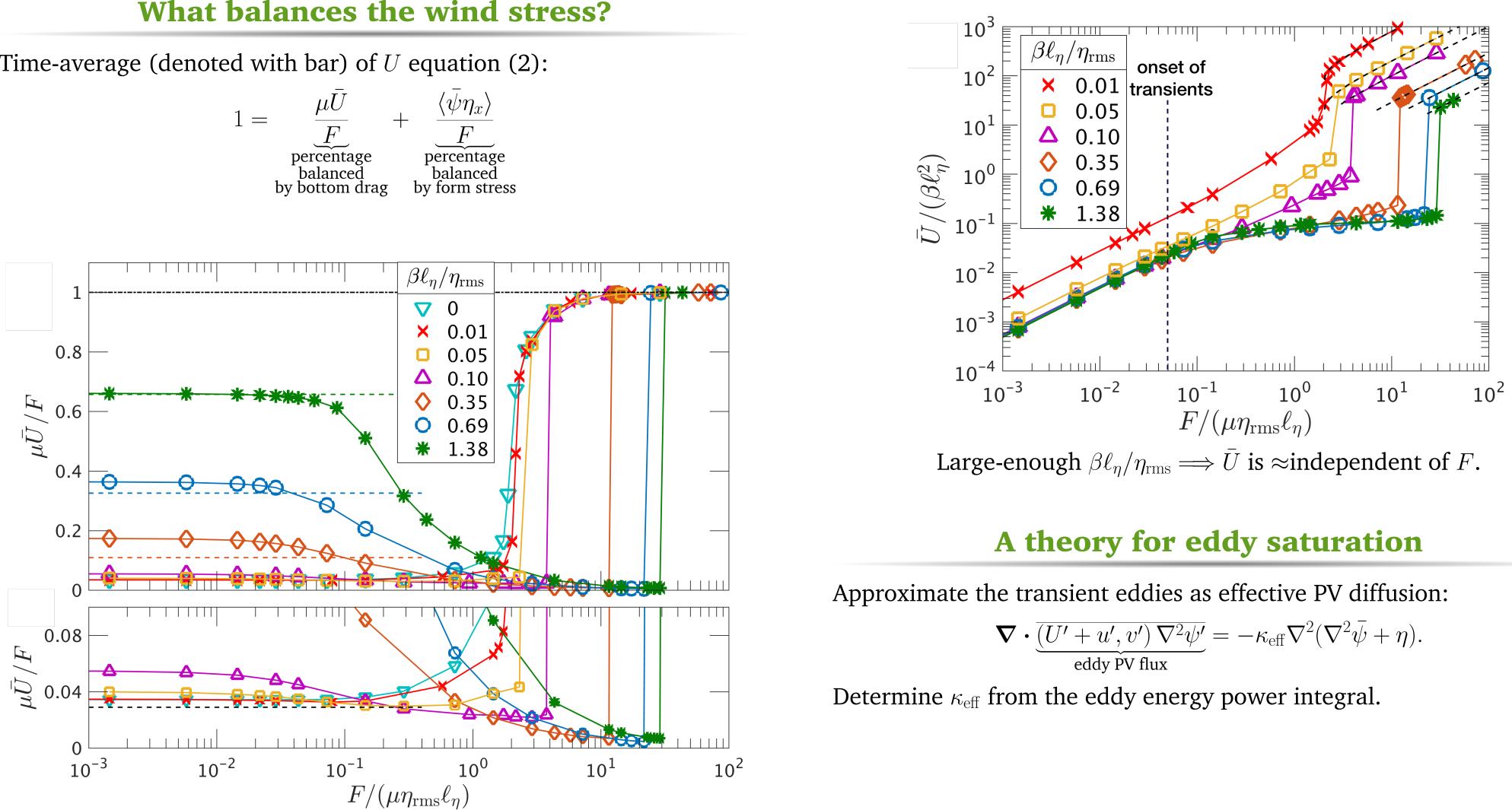
Open vs. closed geostrophic contours

The ratio $\beta \ell_{\eta} / \eta_{\rm rms}$ (= $\beta / \sqrt{\langle |\nabla \eta| \rangle}$) controls whether there exist closed geostrophic contours, i.e. level sets of $\beta y + \eta$.



What balances the wind stress?

Time-average (denoted with bar) of U equation (2):



than ≈ 0.5 .

Weakly and strongly forced solutions (quasilinear – QL)

Assume steady flow. Then (2):

$$F - \mu U - \langle \psi \eta_x \rangle = 0$$

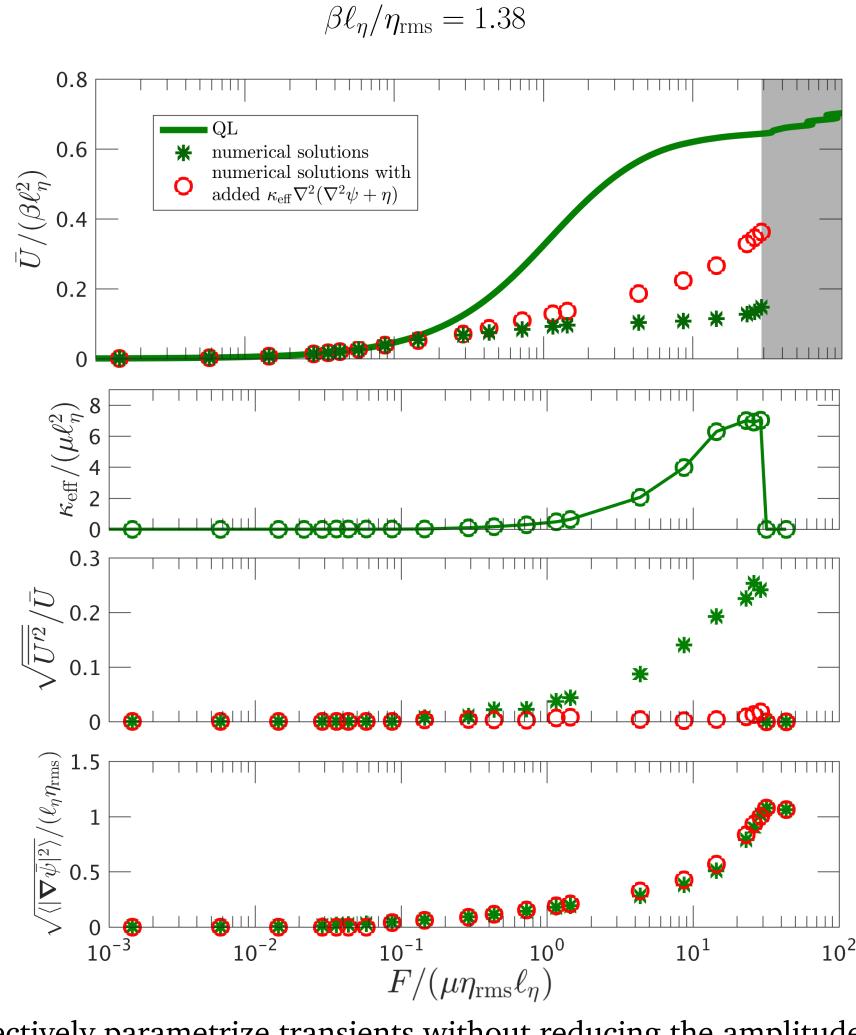
• Weakly forced: neglect quadratic terms $J(\psi - Uy, \nabla^2 \psi)$ in (1): $\mathsf{J}(\psi - Uy, \eta + \beta y) + \mu \nabla^2 \psi = 0.$

• Strongly forced: neglect $J(\psi, \nabla^2 \psi + \eta)$ in (1): $\beta \psi_x + U \nabla^2 \psi_x + U \eta_x + \mu \nabla^2 \psi = 0.$

 \implies obtain scalings for \overline{U} with F. Good agreement with numerics.

Eddy saturation regime

$$abla \cdot \underbrace{(U'+u',v') \nabla^2 \psi'}_{ ext{eddy PV flux}} = -\kappa_{ ext{eff}} \nabla^2 (\nabla^2 \overline{\psi} + \nabla^2 \overline{\psi}) + \nabla^2 \overline{\psi} + \nabla^$$



Effectively parametrize transients without reducing the amplitude of standing eddies.

- periodic model.

Constantinou, N. C. and Young, W. R. (2016) Beta-plane turbulence above monoscale topography, J. Fluid Mech. (submitted, arXiv:1612.03374)

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The effective PV diffusion approximation is good for $\beta \ell_n / \eta_{\rm rms}$ larger

Conclusions

There exists flow regimes with flow depending:

– only on statistical properties of topography (large $\beta \ell_{\eta}/\eta_{\rm rms}$), – on the geometrical structure of topography (small $\beta \ell_{\eta}/\eta_{\rm rms}$).

• Existence of eddy saturation regime in this barotropic, doubly

explanation: effective PV homogenization theory.

• Large zonal transport ensues as wind increases.

explanation: enstrophy power integral imposes the need for such transition as wind stress crosses a threshold (see paper).



