



Australian
National University

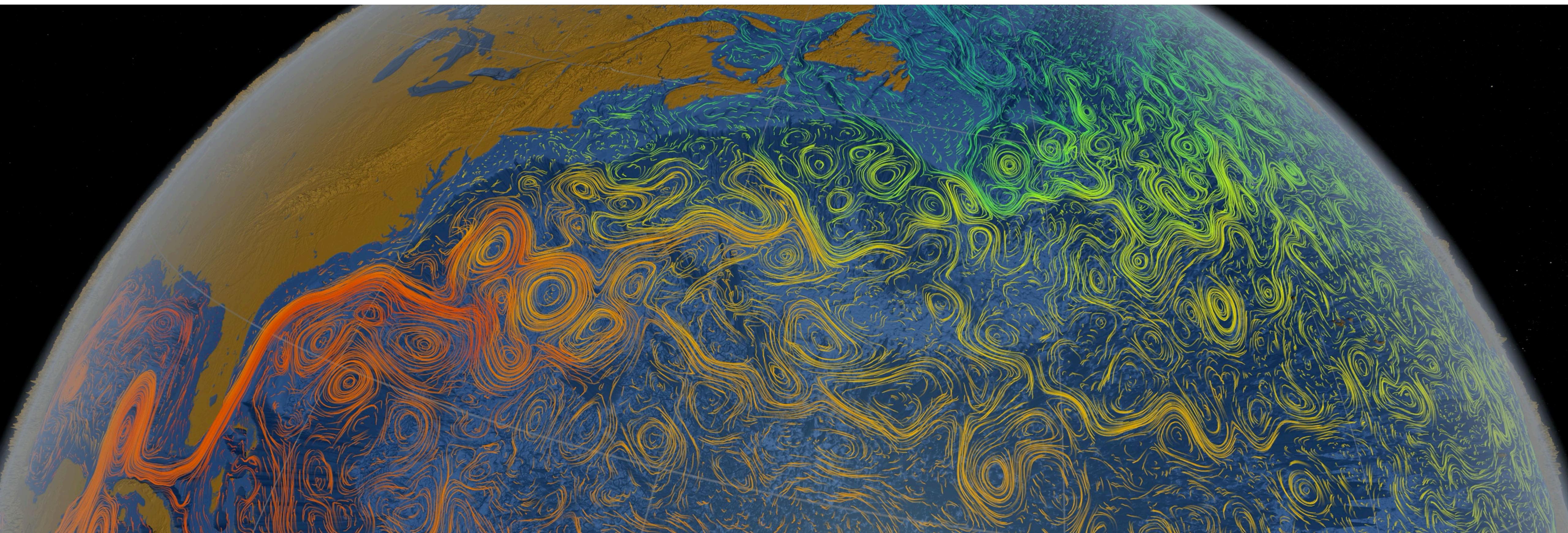
A data-driven approach for developing and calibrating a parametrization for mesoscale eddy fluxes

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Australian Government
Australian Research Council

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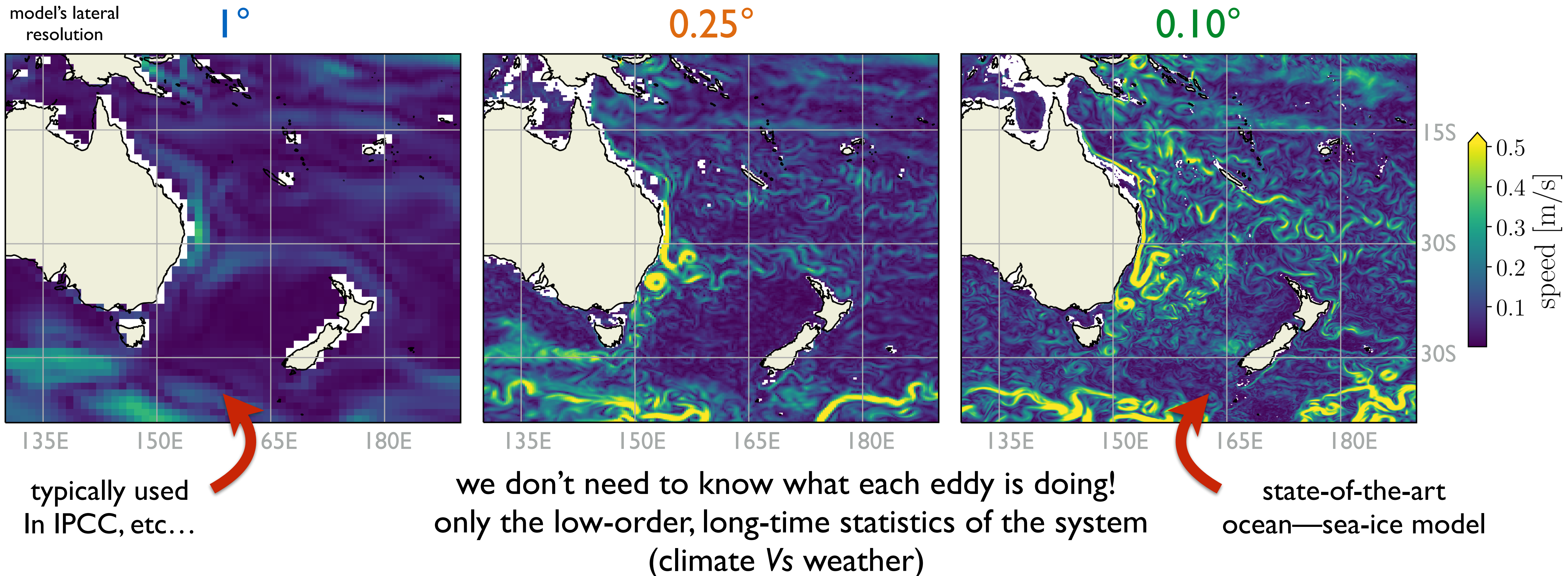
Visualization using output from the MIT/JPO project
Estimating the Circulation and Climate of the Ocean, Phase II (ECCO2)

Ocean Sciences Meeting 2022

Credit: NASA/Goddard Space Flight
Center Scientific Visualization Studio

can we make the **coarse model** feel the effect
of the flow details that it does not resolve?

[in technical terms: 'eddy parameterisation']





how eddies affect tracers?

tracer dynamics (e.g. heat, salt, ...)

$$\frac{\partial c}{\partial t} + \mathbf{u} \cdot \nabla c = \kappa \nabla^2 c$$

Reynolds decomposition

$$c = \bar{c} + c' \quad \text{resolved} \quad \text{unresolved eddies}$$
$$\mathbf{u} = \bar{\mathbf{u}} + \mathbf{u}'$$

$$\underbrace{\frac{\partial \bar{c}}{\partial t} + \bar{\mathbf{u}} \cdot \nabla \bar{c} = \kappa \nabla^2 \bar{c}}_{\text{dynamics the model solves for}} - \underbrace{\nabla \cdot (\overline{\mathbf{u}'c'})}_{\text{subgrid eddy fluxes}}$$

$\overline{\mathbf{u}'c'}$ eddy tracer flux

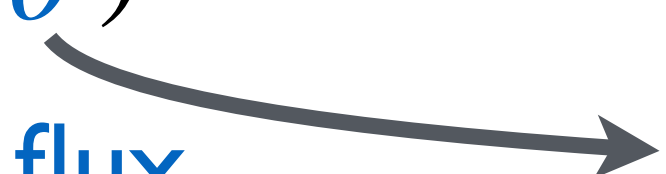
parametrization

express **eddy tracer flux** in terms of the **resolved fields**

$$\overline{u'c'} = \mathcal{F}(\overline{u}, \overline{c}, \dots; \theta)$$

eddy tracer flux eddy tracer flux parametrization

free parameters
($\kappa_{\text{GM}}, \kappa_{\text{Redi}}, \dots$)



how do we come up with \mathcal{F} ?

how do we come up with parametrizations?

get inspired by data
(model output,
observations,...)



derive a model
from physical intuition
(usually involves some
free parameters)



calibrate free parameters
to match data

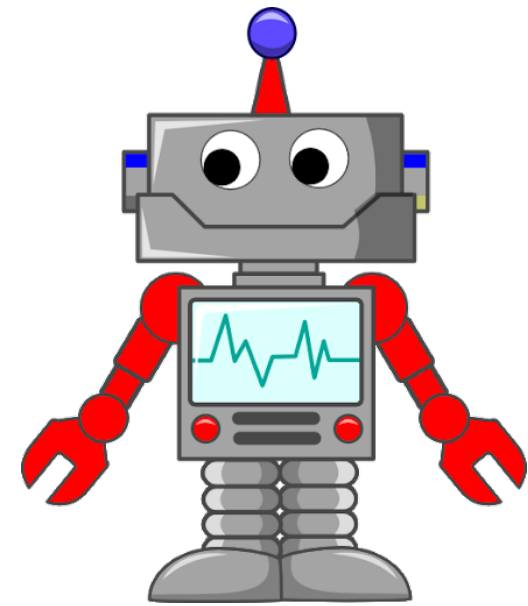


implement in climate model
and produce IPCC reports, etc



how do we come up with parametrizations? and how machines can help?

get inspired by data
(model output,
observations,...)



derive a model
from physical intuition
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calibrate free parameters
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a proof of concept

take the standard isoneutral diffusion parametrisation (“Gent-McWilliams”)



model derivation



free parameters



calibration of free parameters



isoneutral diffusion

Eddies mix tracers.

But it costs (potential energy) to mix across isopycnals.

downgradient flux
locally aligned with neutral direction

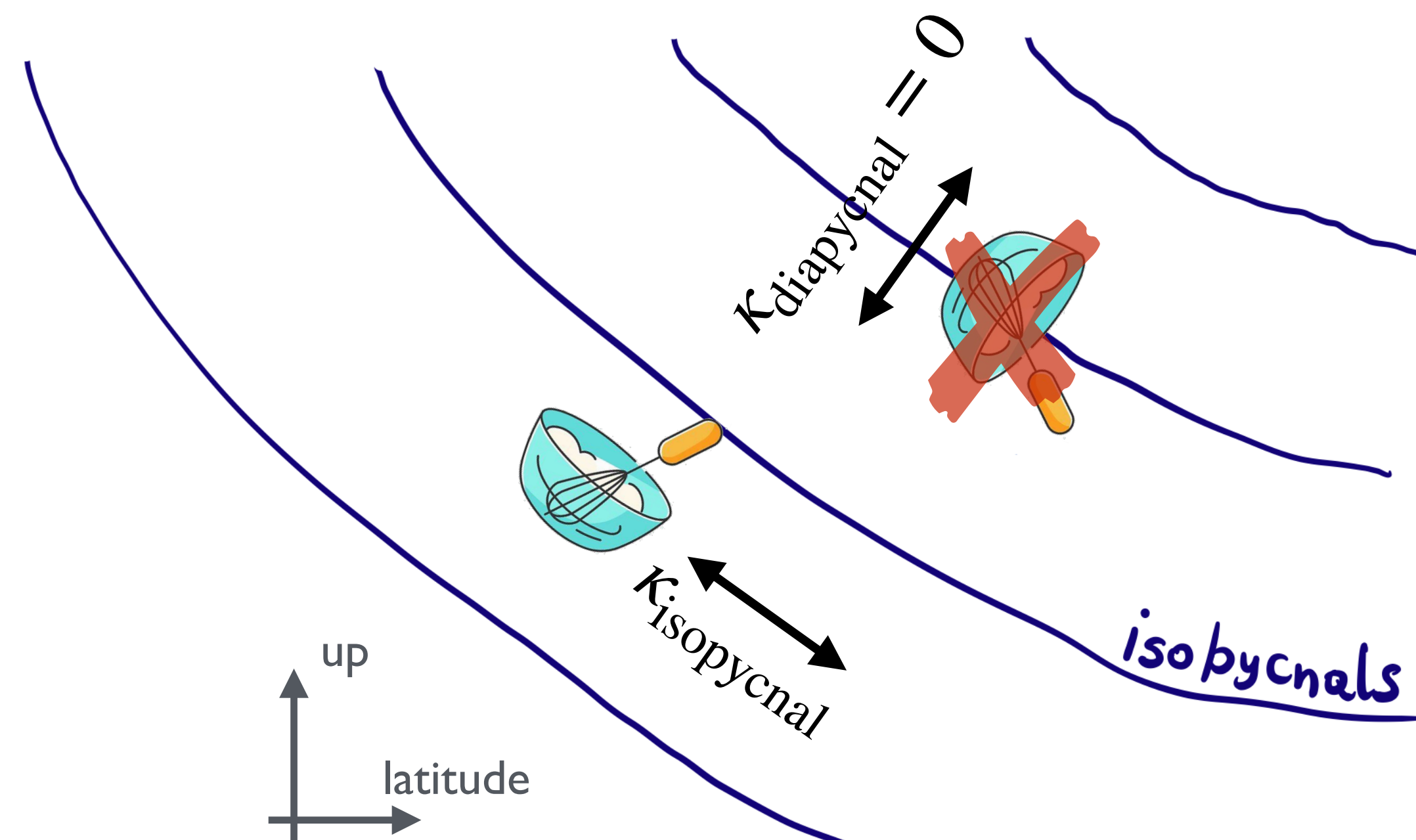
$$\overline{u'c'} \approx -\mathbb{K}_{\text{eddy}} \cdot \nabla \bar{c}$$

3x3 tensor that rotates to
neutral-cross neutral directions

$$\overline{u'c'} \approx -(\mathbb{K}_{\text{GM}} + \mathbb{K}_{\text{Redi}}) \cdot \nabla \bar{c}$$

skew flux
modeling
stirring along
isopycnals

tracer
diffusion
along
isopycnals





isoneutral diffusion

Eddies mix tracers.

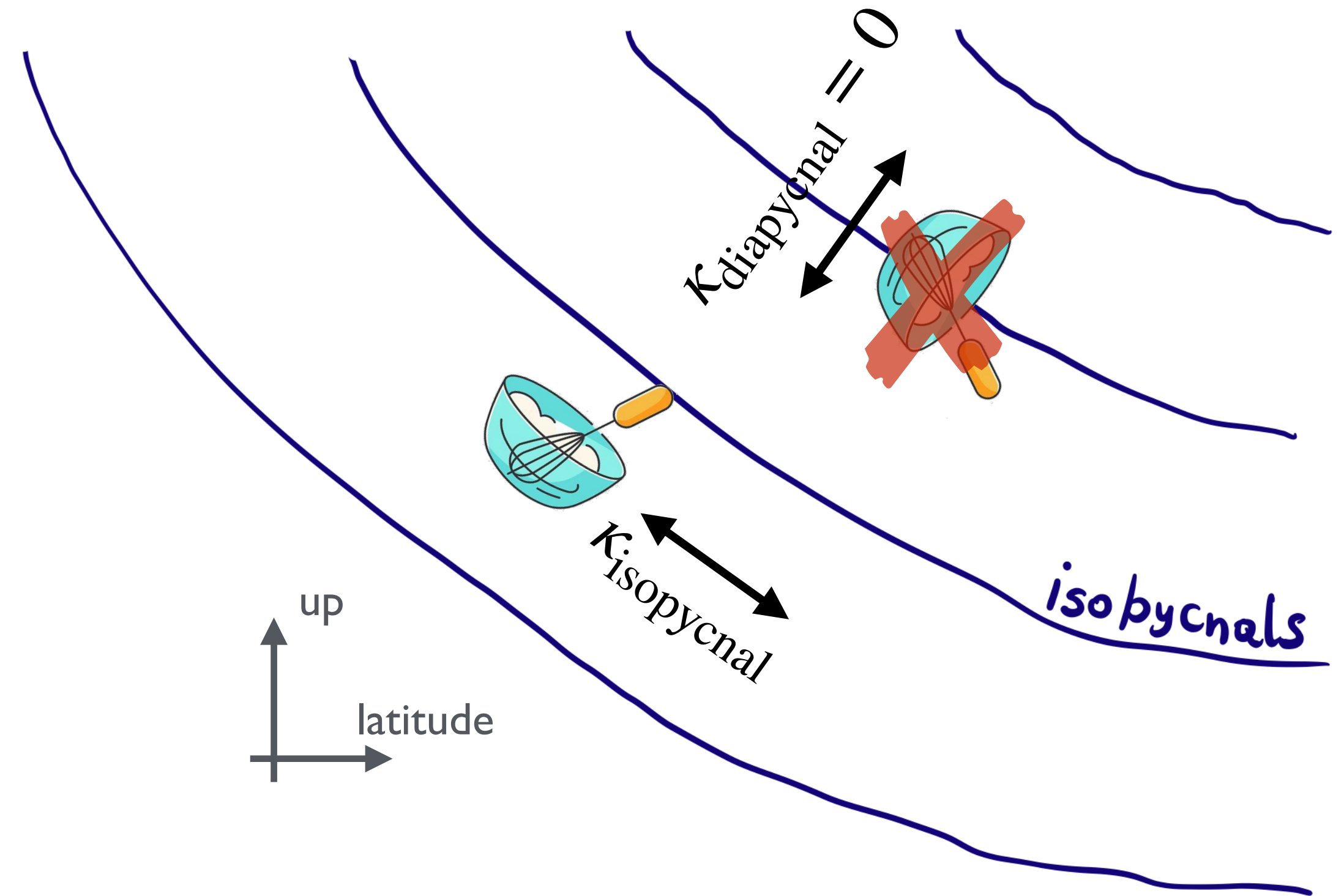
But it costs (potential energy) to mix across isopycnals.

$$\overline{u'c'} \approx - (\kappa_{\text{GM}} + \kappa_{\text{Redi}}) \cdot \nabla \bar{c}$$

skew flux
modeling
stirring along
isopycnals

tracer
diffusion
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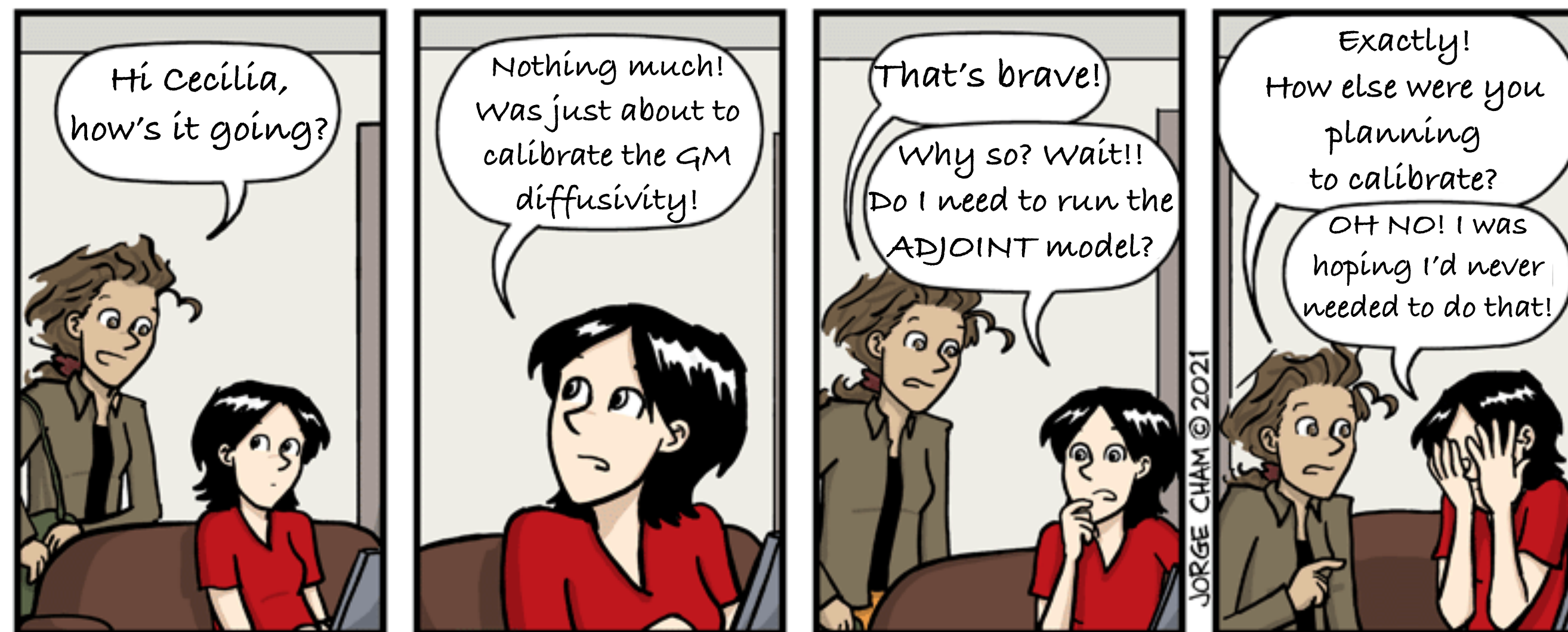
Two free parameters $\rightarrow \kappa_{\text{GM}}$ and κ_{Redi} diffusivities



calibration

*“All agree that calibration is great!
But most don’t do it in a systematic manner
because it is so cumbersome!”*

— adage



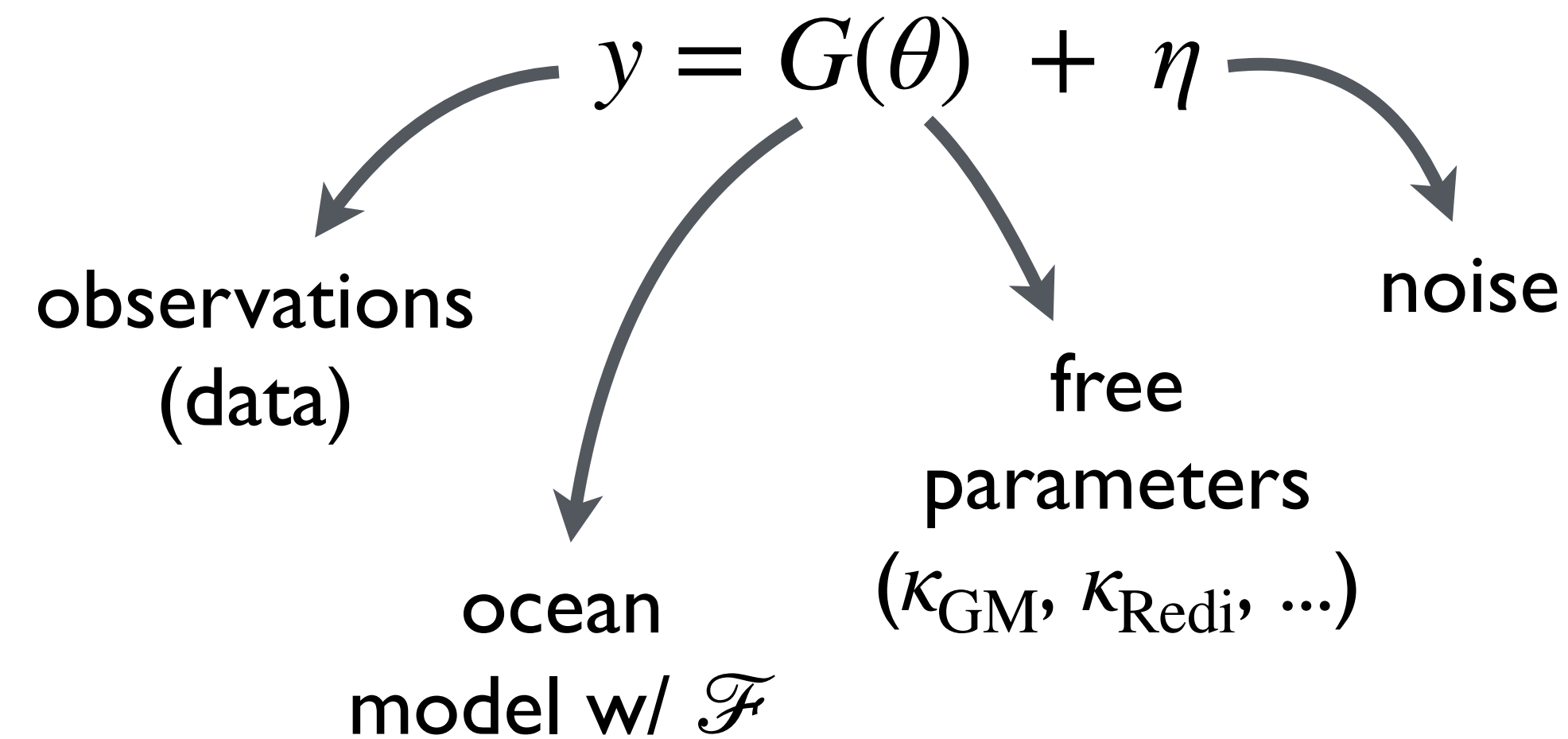
adopted from WWW.PHDCOMICS.COM
and slightly modified



*derivative-free Bayesian optimization
using ensemble Kalman filters*

Ensemble Kalman Inverse process

Derivative-free ensemble optimization method
that seeks to find the optimal parameters θ for inverse problem



find free parameters θ that minimize $\|y - G(\theta)\|$

Calibration is done *online* by running *ensembles* of *forward* model runs





open-source software development



[Oceananigans.jl](#) Public

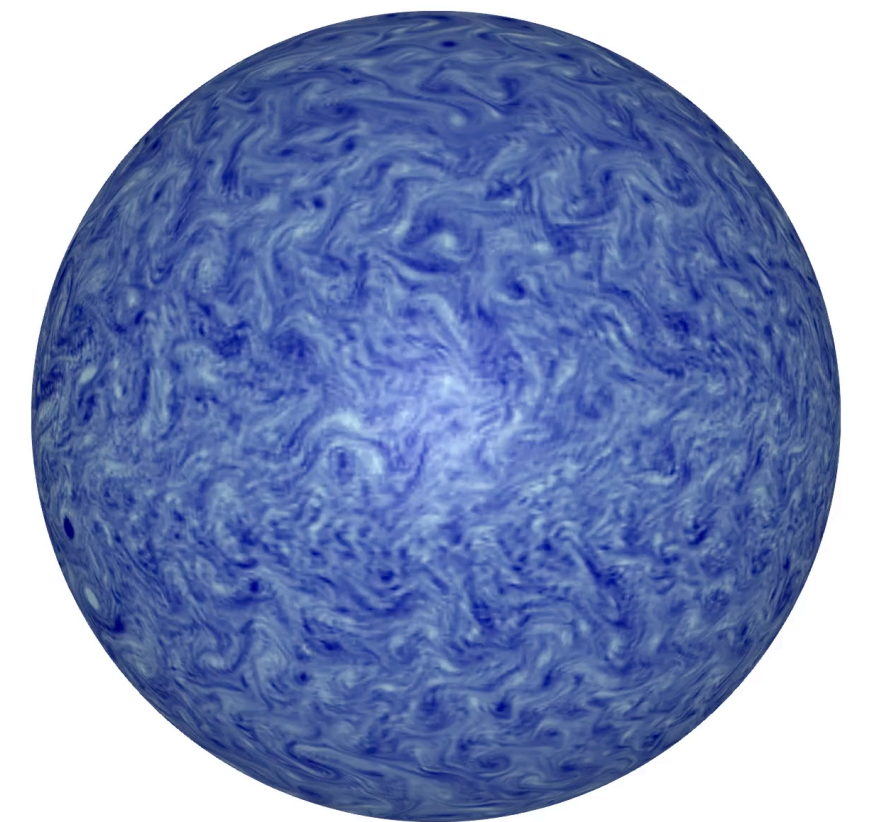
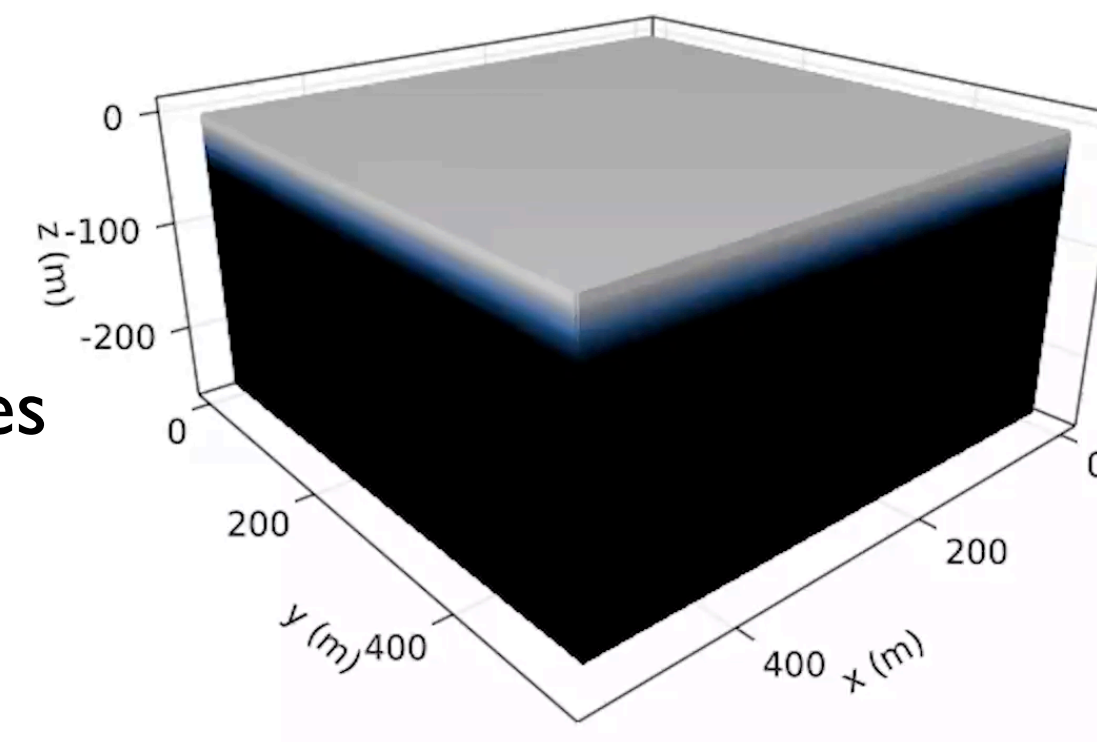
 Julia software for fast, friendly, flexible, data-driven, ocean-flavored fluid dynamics on CPUs and GPUs

 Julia  581  MIT  105  221 (3 issues need help)  21 Updated 4 hours ago

GPU-friendly finite-volume calculations on staggered grids



- Nonhydrostatic + closures for large eddy simulation
- Hydrostatic w/ free surface + boundary layer, mesoscale closures
- **Model ensembles: 1D columns, 2D slices**



```
julia> N² = α * ∂z(T) - β * ∂z(S)
```

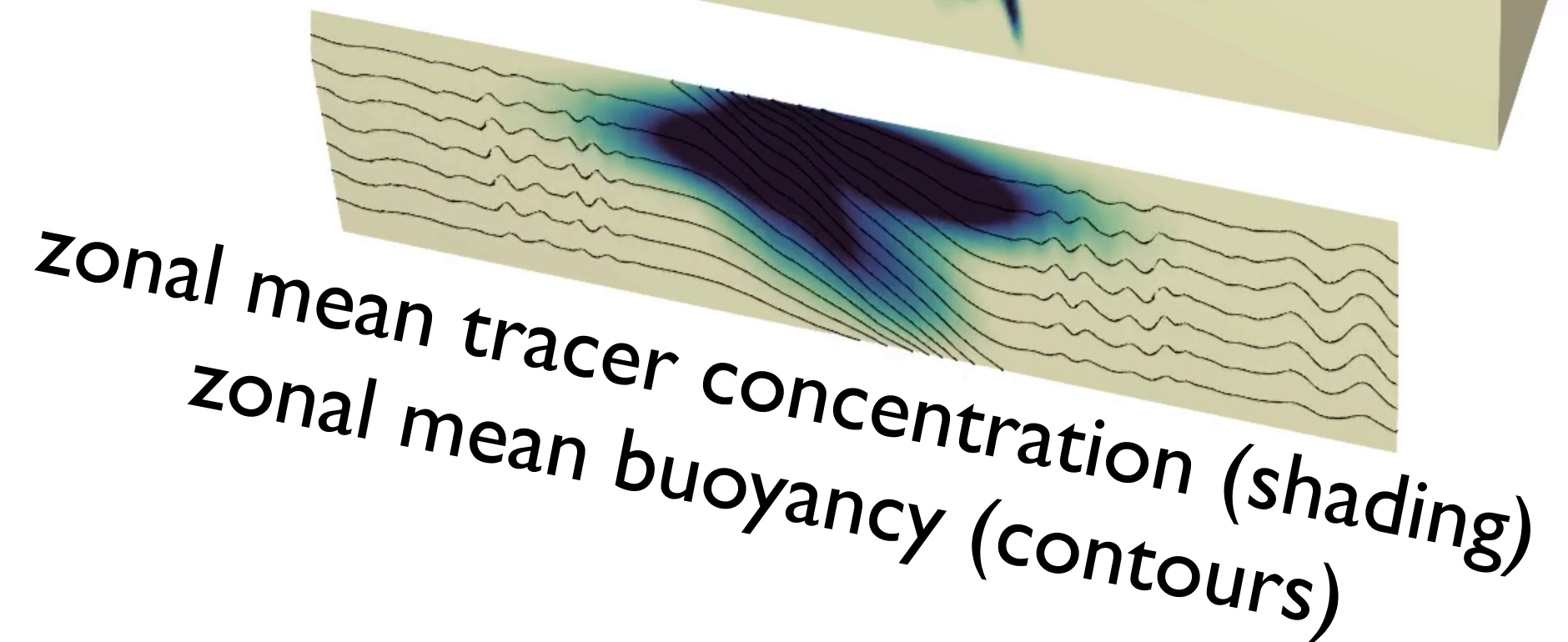
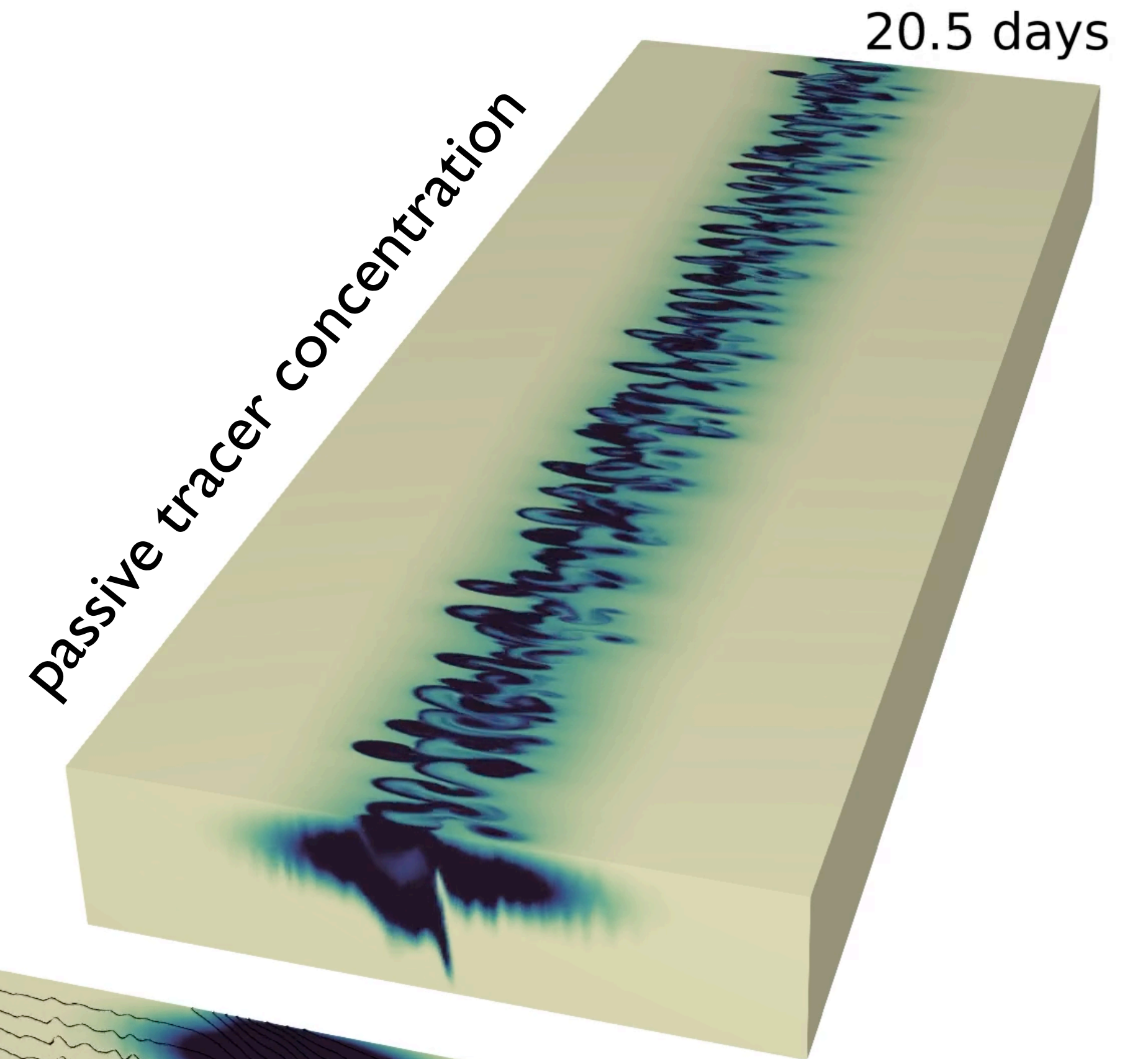
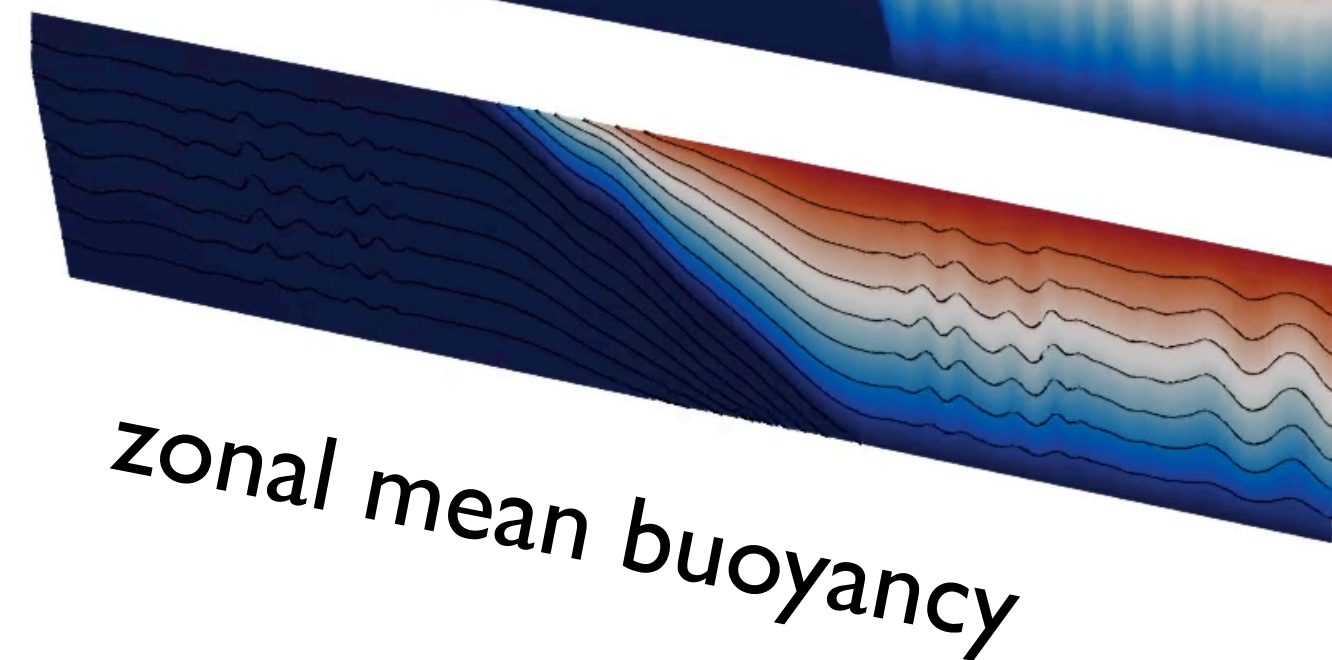
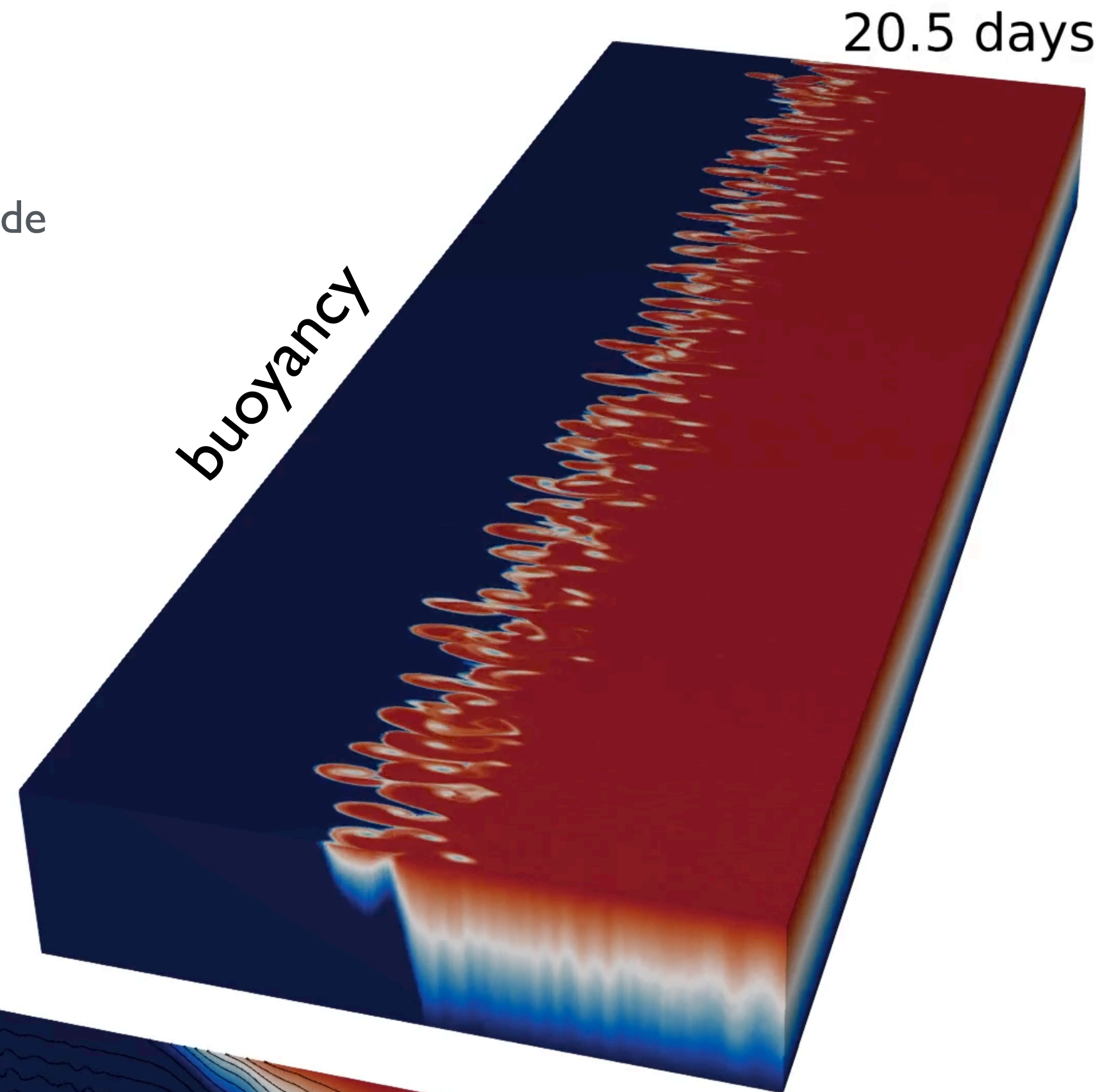
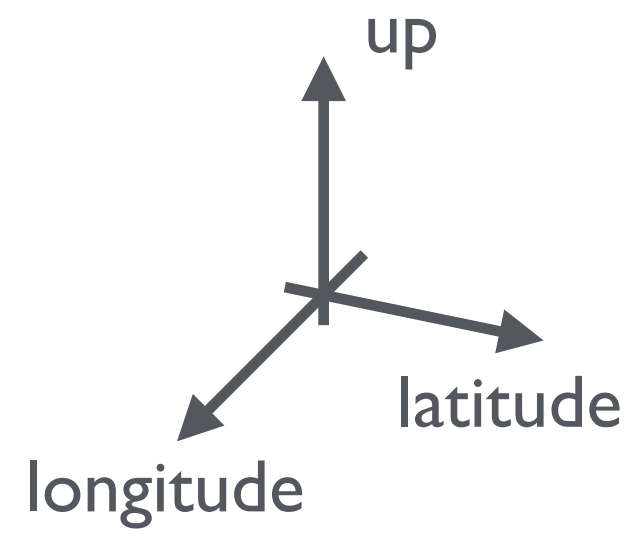
[OceanTurbulenceParameterEstimation.jl](#) Public

Estimation of turbulence closure parameters for ocean models using Ensemble Kalman Inversion.

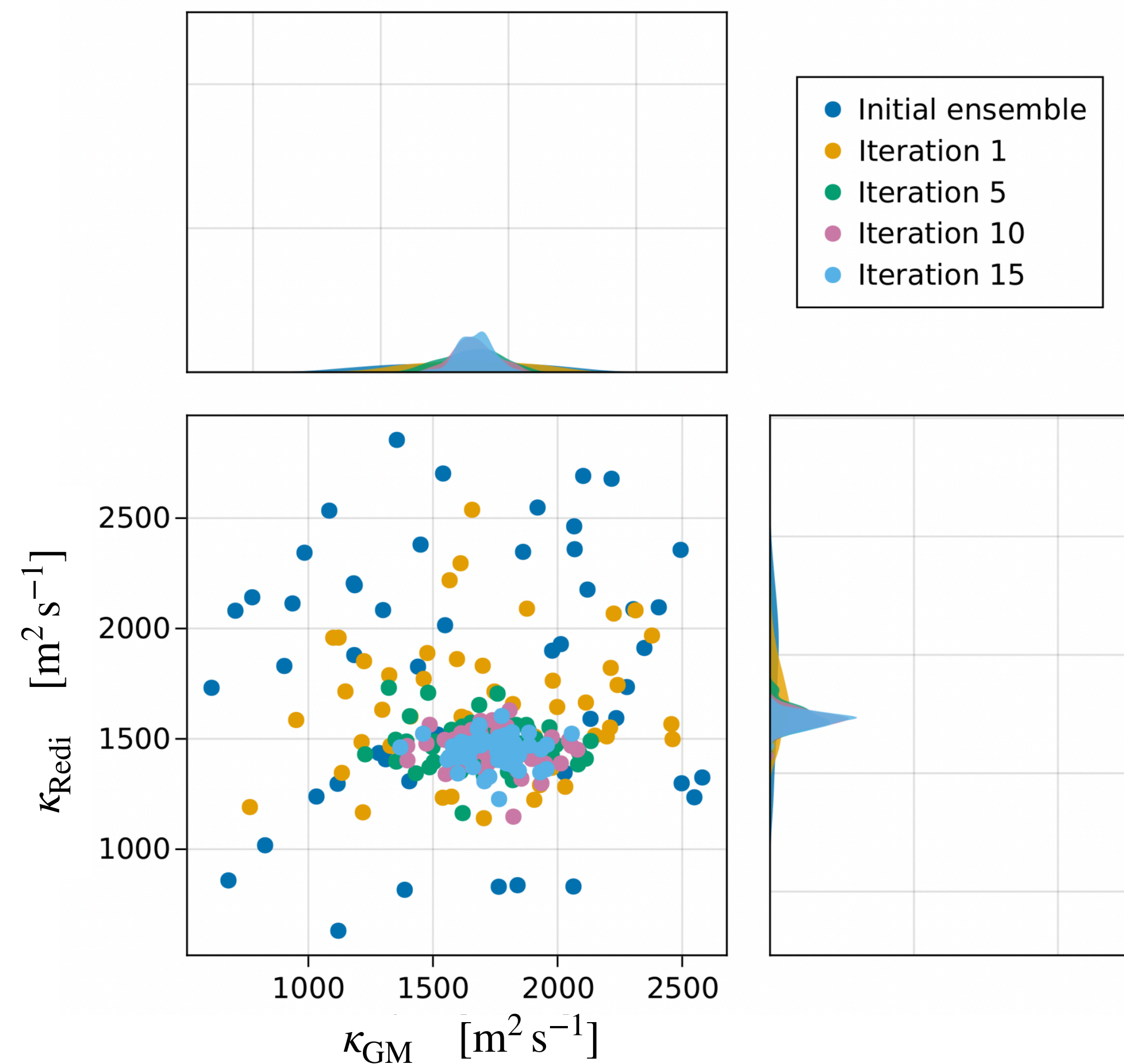
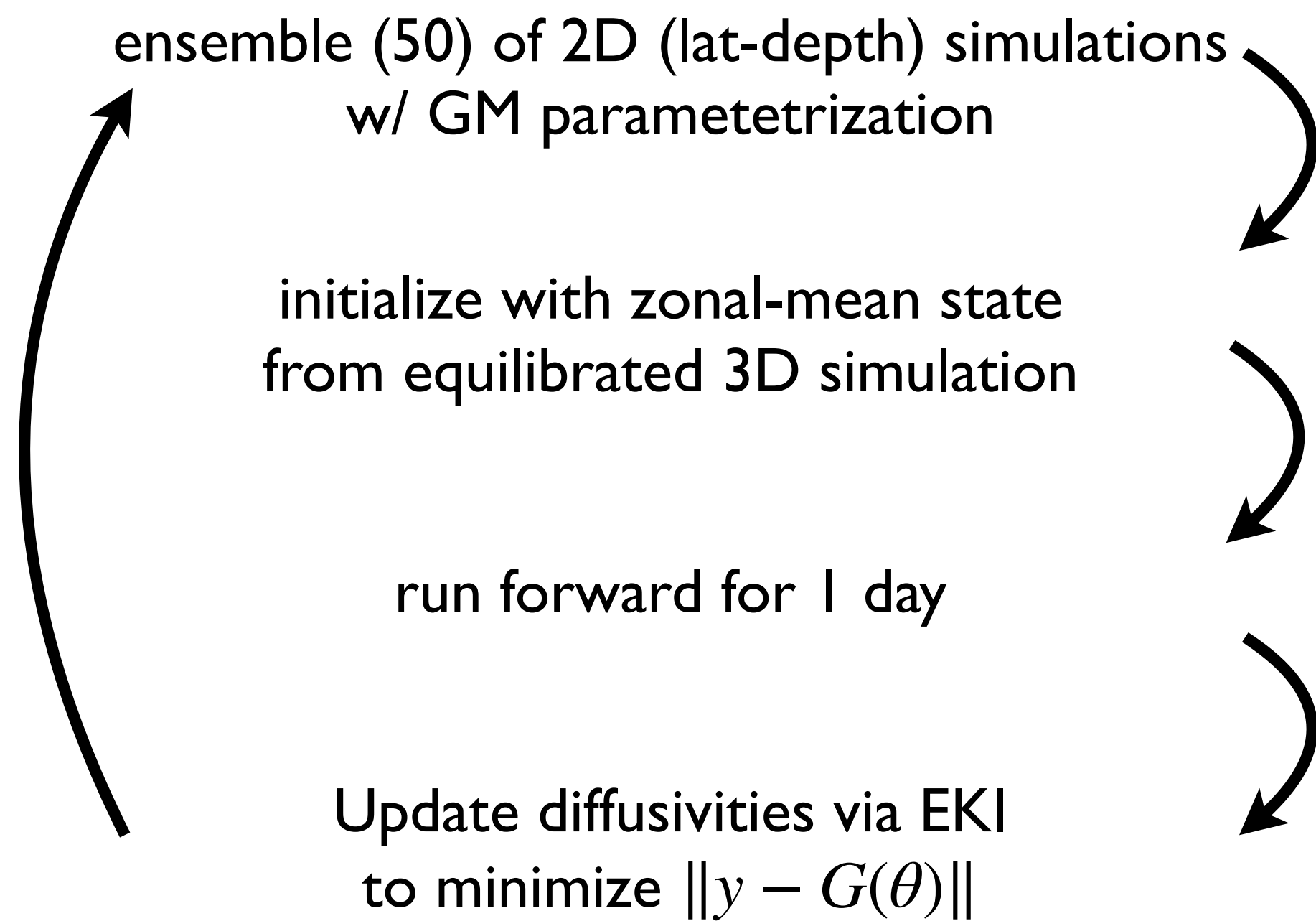
 Julia  5  MIT  2  19  4 Updated 9 minutes ago



baroclinic adjustment of a front



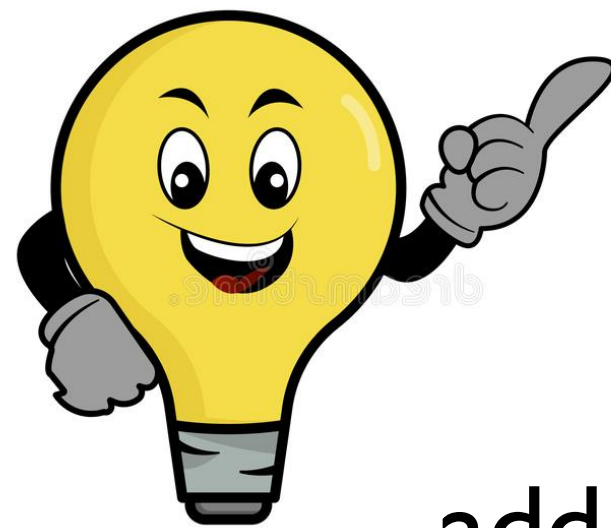
model diffusivities calibration using Ensemble Kalman Inverse process



OK, so what?

we can easily calibrate free parameters of a turbulence closure

we can even calibrate *simultaneously* across various scenarios
and find optimal parameters that are robust

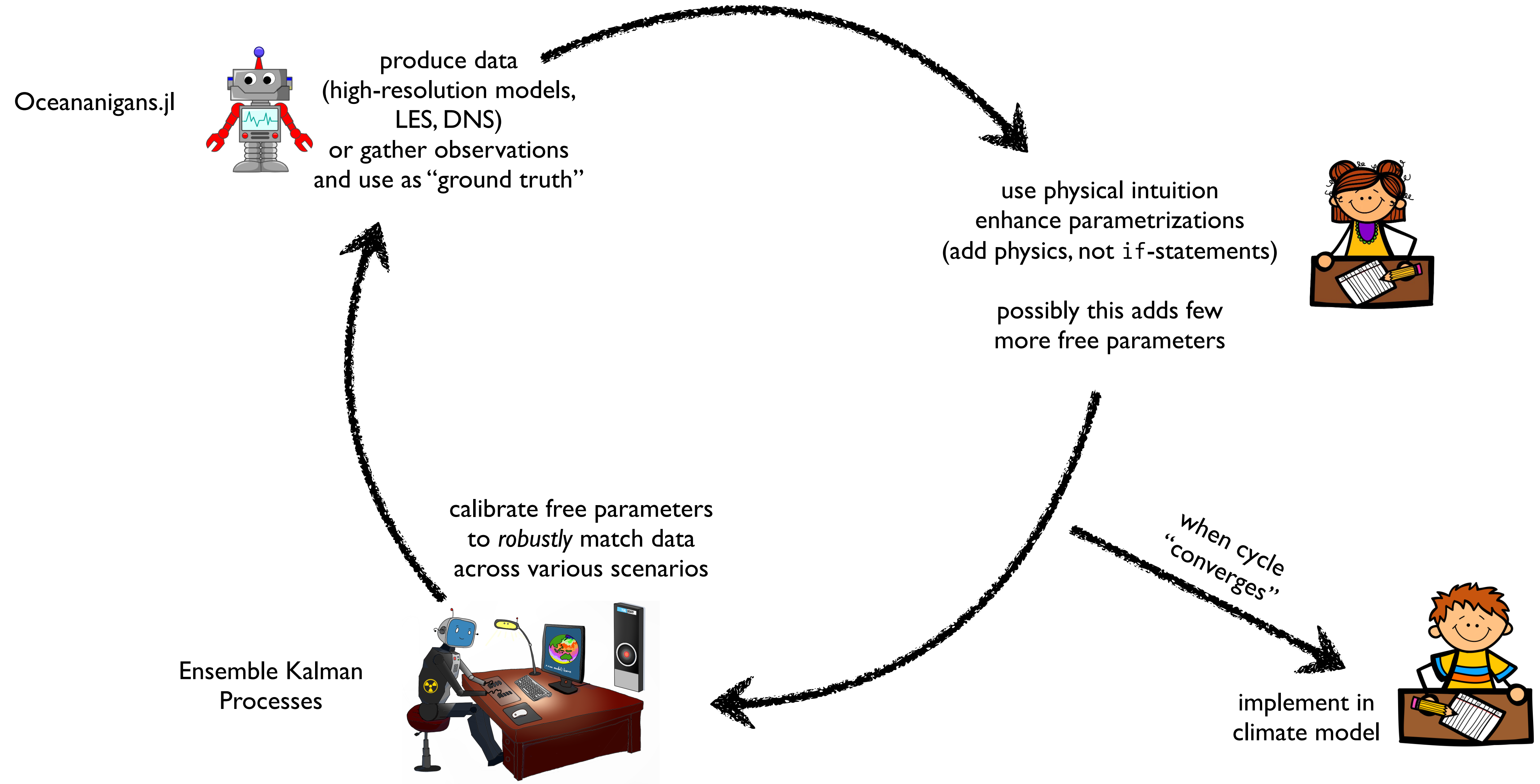


add depth/time/anything dependence in free parameters is trivial

any parametrization obtained this ways
is, *by construction*, numerically stable
when added back to the model



but that's only the beginning



the music in this talk was from the song

“From little things big things grow”

by



Paul Kelly